AN APPROACH TO THE PARAMETRIC DESIGN OF ION THRUSTERS†

Paul J. Wilbur††
Colorado State University
Fort Collins, Colorado 80523, U.S.A.

and

John R. Beattie* and Jay Hyman, Jr.**
Hughes Research Laboratories
Malibu, California 90265, U.S.A.

ABSTRACT

A methodology that can be used to determine which of several physical constraints can limit ion thruster power and thrust, under various design and operating conditions, is presented. The methodology is exercised to demonstrate typical limitations imposed by grid system span-to-gap ratio, intragrid electric field, discharge chamber power per unit beam area, screen grid lifetime and accelerator grid lifetime. Other limitations on power and thrust for a thruster defined by typical discharge chamber and grid system parameters when it is operated at maximum thrust-to-power are discussed. It is generally recognized, however, that operational objectives such as optimization of payload fraction or mission duration can be substituted readily for the thrust-to-power objective and that the methodology can be used as a tool for mission analysis.

INTRODUCTION

Ion thrusters are very attractive propulsion devices not only because of their high efficiency and high specific impulse capabilities but also because they afford designers and potential users a great deal of design and operational flexibility. It is generally recognized, however, that operational flexibility (e.g. throttleability) carries with it a price of a greater system complexity that may not be justifiable for many missions and it should be noted that design flexibility also has its unattractive aspects. It can for example conjure up impressions, particularly in the minds of those who do not work directly with ion thrusters, that they are too complex. In order to overcome this concern, the work described herein has been undertaken and a framework within which ion thruster performance and design information can be presented in a simple, easily understood way has been sought. It is hoped that this methodology can be used to facilitate communication, teaching, and an identification of the most productive areas for research and development in support of a variety of propulsion system objectives.

The development of this methodology might be pursued in terms of empirical relationships following the techniques used by Byers and Rawlin1 and by Byers2 but the desire to use it for teaching purposes coupled with the fact that basic models describing ion thrusters have become available since their works was published, has prompted us instead to base the development on basic physical models. Where parameters are required in this development to accommodate non-ideal behavior, every attempt has been made to use parameters that are physically meaningful, commonly used and theoretically based. The objective of this paper is to present a methodology that can be used to establish a link between thruster design, operational and mission parameters in order to determine which of many possible performance-limiting phenomena will dominate in a particular situation. A second objective is to establish a technique that can be used to present information on this subject in a manner that is both easy to visualize and understand.

THEORY

The canonical design variables associated with an ion thruster are the specific impulse at which it operates (Isp), its beam area (Abeam) and its beam power (Pbeam). Generally, one would want to prescribe the specific impulse and beam area of a device and then determine the beam power at which it could be operated under a given set of design, operational and mission constraints, so in this development specific impulse and beam area will be treated as independent variables and beam power will be treated as the dependent variable.

Examples of physical constraints which have been found to limit the beam power at which a thruster can operate include:

Grid system span-to-gap ratio. This constraint is determined by ones ability to hold grids close together in an environment of thermally induced distortion and in some situations significant electrostatic attraction. It is influenced greatly by mechanical design and fabrication considerations and while a value of 600 might be considered a reasonable limit for conventional circular grids, the use of intragrid supports or non-circular (e.g. annular or rectangular grids) could facilitate substantial increases above 600.

Intragrid electric field. Excessively high electric fields between the screen and accelerator grids of a thruster result in electrical breakdown and an inability to extract an ion beam. This limit is influenced by such factors as the surface finish and uniformity of the intragrid spacing and typical values in operating thrusters have generally been about 2 kV/m, although much higher values have been reported.

Discharge power per unit beam area. This is actually a heat transfer limit that is imposed because components such as magnets, anodes or grids can overheat if the heat removal rate is inadequate. This constraint could be formulated in terms of specific heat transfer limitations for particular components but for the illustrative purposes of this paper, it will be assumed that the allowable discharge power scales directly with beam area and that a limit in the range 15 to 30 kW/m² is reasonable.

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*Head, Plasma Sources Section, Ion Physics Dept., Member AIAA.
†Professor, Dept. of Mechanical Eng., Member AIAA.
**Manager, Ion Physics Dept., Member AIAA.
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Screen grid lifetime. The lifetime of the screen grid as well as other components exposed to the discharge plasma is limited by the process of ion-induced sputter erosion. Typically grids and other components have been designed to have lifetimes in the range of 10^4 to 2 x 10^4 hours. These lifetimes are influenced by the materials and ions involved and by the discharge voltage.

Accelerator grid lifetime. The accelerator grid is exposed to small currents of high energy, charge-exchange ions that limit its lifetime through sputter erosion. This grid is typically designed to have a lifetime in the same 10^4 to 2 x 10^4 hr range that the screen grid has.

The above list of constraints on ion thruster design is not exhaustive, but they represent constraints that have been encountered and they can be used for purposes of illustration.

A trade-off exists between the propellant and power requirements for an ion thruster and for this reason a preferred operating point or operational objective exists. The one selected influences the severity of each of the design constraints identified above. Once an objective that requires operation, for example, at the point where the thruster will produce maximum thrust per unit input power or maximum payload fraction on a prescribed mission has been identified, one can define the extent of the power limits cited in the preceding paragraphs. For the purposes of this study it will be assumed that the thruster is to be operated at the point of maximum thrust-to-power, but it should be recognized that this additional input, which could be much more complex, might come for example from an algorithm that optimizes a mission objective.

Mathematical Development

The beam power \( P_B \) produced by an ion thruster is expressed most simply as the product of beam current \( J_B \) and beam (or net accelerating) voltage \( V_B \).

\[
P_B = J_B V_B
\]  

(1)

The beam current in this equation is related to the peak current density being extracted through the grids \( J_{\text{max}} \) and the beam area \( A_B \) through the beam flatness parameter \( IF \) which is defined as the ratio of average-to-peak ion beam current density.

\[
IF = J_B / J_{\text{max}}
\]  

(2)

It is noted that the flatness parameter can be computed for a given discharge chamber using the finite element technique developed by Arakawa.

The maximum current density capability of a grid set is determined by space-charge limitations which may be described approximately using the onedimensionally based Child-Langmuir law.

\[
j_{\text{max}} = \frac{4 e}{9} \left( \frac{2 e}{m_i} \right)^{1/2} \frac{V_B^{3/2}}{I_B} \phi_s \rho_s
\]  

(3)

The permittivity of free space \( \varepsilon_0 \), the electron charge \( e \), and the ion mass \( m_i \) appearing in this equation are known constants and the total accelerating voltage \( V_B \), and the screen grid transparency to ions \( \phi_s \) are at the control of the designer and/or operator. The ion current density enhancement factor \( \phi_s \) is a factor that will be set equal to unity for the purposes of this paper, but it could take on values greater than unity to account for the increased current density capabilities of grids when ions are decelerated, screen grid plasma sheath at non-zero velocities or high energy electrons are injected into the sheath to mitigate the space-charge limitations that develop there.

The final factor in Eq. 3, the effective ion acceleration length \( L_a \), is the one that is limited by span-to-gap and electric field considerations and the imposition of these constraints will be considered in detail next. It will be assumed that the value of \( L_a \) is the same for each aperture set over the entire grid surface for this development.

The total accelerating voltage that appears in Eq. 3 can be eliminated in favor of the beam voltage by introducing the net-to-total accelerating voltage ratio \( R \).

\[
R = \frac{V_B}{V_T}
\]  

(4)

The beam voltage can be related to the specific impulse \( I_s \) by recognizing that the specific impulse is defined as the thrust \( F \) per unit weight flowrate of propellant \( \rho g \).

\[
I_s = \frac{F}{\rho g}
\]  

(5)

and that the ion exhaust velocity \( U \) is related to the beam voltage through the conservation of energy expression

\[
V_B = m_i U^2 / 2.
\]  

(7)

In Eq. 6 the product of propellant mass flowrate \( \dot{m} \) and propellant utilization efficiency \( \eta_p \), which is the first bracketed term, represents the flowrate of thrust producing (high velocity) propellant and the second bracketed term represents the effective jet velocity of the beam ions along the thruster axis. This second term includes two thrust correction factors, one \( F_i \) that reflects the fact that many ions will emerge from the grid system on divergent trajectories and a second \( \eta_p \) that accounts for the fact that Eq. 7 describes the velocity of singly charged ions only when in fact some multiply charged ions will generally be produced and extracted.

Combining Eqs. 3, 6 and 7 the desired expression for beam voltage in terms of specific impulse is obtained.

\[
V_B = \frac{m_i}{2 \rho g} \left( \frac{I_s}{\eta_p F_i} \right)^{1/2}
\]  

(8)

and this may be combined with Eqs. 1 through 4 to obtain

\[
P_B = \frac{\rho g}{9} \left( \frac{2 e}{m_i} \right)^{1/2} \frac{V_B^{3/2}}{I_B} \phi_s \rho_s \left( \frac{I_s}{\eta_p F_i} \right)^{1/2}
\]  

(9)

Equation 9 defines the maximum power constraint associated with the ion extraction process for an ion thruster as a function of its beam area and the specific impulse at which it is to operate. Two physical constraints, one associated with the allowable span-to-gap ratio and the other with the maximum allowable electric field between the grids, actually evolve from this equation through the effective ion acceleration length \( L_a \). The fact that propellant utilization appears in the equation also serves as a reminder that an operational objective must be defined before unique limiting values of beam power can be computed as a function of specific impulse and beam area for these two physical constraints.

Span-to-Gap Ratio Constraint

The allowable span-to-gap ratio \( N \) associated with traditional grid sets is the grid diameter-to-spacing ratio. In order to accommodate non-circular beam cross sections, however, this ratio will be
DOWNSTREAM

defined here using an equivalent beam diameter and the grid separation will be given by the expression

$$I_B = \frac{4 \alpha \bar{A} \omega}{N}$$

(10)

The preferred ion acceleration length for use in Eq. 9 (which is based on one-dimensional theory) would be the one that would yield the beam current density actually extracted from screen/accel grid aperture pairs in what is really a two-dimensional process. One value of $I_d$ that should come close to doing this is illustrated in Fig. 1 and examination of the geometry of this figure suggests that $I_d$ is related to the grid separation distance given by Eq. 10 through the expression

$$I_d = \sqrt{t_s + \frac{I_e}{E} + \frac{d_s}{4}}$$

(11)

It should be noted here that Eq. 11 differs from the traditional equation for $I_d$ used to compute perversances in that it accounts for the screen grid thickness ($t_s$). If the screen grid thickness is left out of this expression, the implication is that the screen hole sheath positions itself close to the downstream edge of the screen grid. Aston has shown, however, that this sheath tends to position itself near the upstream edge of the hole under normal operating conditions and Eq. 11 is therefore considered correct.

Equations 9, 10, and 11 can be combined to define the maximum beam power at which a thruster with a beam area $A_B$ and a span-to-gap ratio $N$ can be operated at prescribed specific impulses provided an operational objective, a screen grid thickness ($t_s$) and a screen hole diameter ($d_s$) are specified. For this illustrative study these latter two parameters have been defined by specifying a grid separation-to-screen hole diameter ratio ($I_d/d_s$) and screen grid thickness of unity and 0.0085 $\bar{A}$ respectively.

Discharge Chamber Thermal Constraint

If the power required to operate a discharge chamber becomes too great, such failures as those associated with magnet, screen grid or anode overheating could occur. Of course, the allowable discharge power would scale with thruster size and a review of limiting discharge powers on thrusters having various diameters has suggested that it is probably the discharge power per unit beam area ($P_B/A_B$) that defines this constraint.

The discharge power can be expressed in terms of the energy cost of a beam ion ($\epsilon_B$) through the equation

$$P_B = \frac{\epsilon_B}{A_B}$$

(13)

Combining Eqs. 1, 8 and 13 one can obtain

$$P_B = \frac{\epsilon_B}{A_B}$$

(14)

The beam ion energy cost appearing in this equation can be computed using Brophy's model in the form

$$\epsilon_B = B_0 \left(1 - \eta_u \right)$$

$$+ \frac{eV_0}{B}$$

(15)

where the baseline plasma ion energy cost ($\epsilon_0$) can be computed when the propellant and discharge voltage ($V_D$) are prescribed and the extracted ion fraction ($\eta_u$) and the fraction of the ions produced that go to cathode potential surfaces ($f_e$) can be determined when the magnetic field and electron source location are specified.  The parameter $B_0$ is given by

$$B_0 = \frac{4 \alpha \bar{A} \omega}{m_c}$$

(16)

with Eqs. 2 through 7 to obtain

$$\eta_u = \frac{J_1 m_c}{m_e}$$

(17)

Equations 14, 15, 16 and 18 when combined with an operational objective yield the beam power/beam area/specific impulse surface that defines the discharge power per unit beam area constraint.

Screen Grid Lifetime Constraint

Although the screen grid is assumed to be the life limiting component subjected to sputter erosion in this paper, additional constraints pertaining to other components that are subjected to ion bombardment could impose similar constraints. They would be incorporated into the analysis in the same way as the one developed here for the screen grid. If the screen grid lifetime is considered to have expired when a fraction $\gamma$ of its initial thickness $t_s$ has been sputtered away then this lifetime will be given by

$$t_s = \frac{1}{\gamma}$$

(18)
where $\rho$ and $M$ are the density and molecular weight of the grid material, $N_a$ is Avagadro's number, $J_+^\text{c}$ and $J_+^\text{c}$ are the singly and doubly charged ion current densities striking the grid and $S_+^\text{c}(V_e)$ and $S_+^\text{c}(2V_e)$ are the sputtering yields of the grid material for singly and doubly charged ions evaluated respectively for ions with energies equal to the discharge voltage and twice the discharge voltage. Recognizing that the grid will sputter most rapidly at the point of maximum current density $(J_+ = J_+^\text{c})$, Eqs. 1, 2 and 8 can be combined with Eq. 19 to obtain

$$P_B = \frac{m_n N_\text{p} \gamma_\text{p} \gamma_\text{c} \int F_A \rho \gamma_\text{c} \eta_\text{d} \alpha \left[ \frac{T_{\text{p}} S_{\text{co}}}{n_e F_e \alpha} \right]^2}{2 r_\text{p} M [S_+^\text{c}(V_e) + 0.5 J_+^\text{c} S_+^\text{c}(2V_e)]}.$$

The doubly-to-singly charged ion current density ratio $(J_+^\text{c}/J_+^\text{c})$ appearing in this equation is a strong function of discharge operating conditions and is given by

$$J_+^\text{c}/J_+^\text{c} = \frac{2 Q_0^+ N_\text{p} \gamma_\text{p} \gamma_\text{c} + 0.83 V_e}{V_0} \frac{\eta_\text{d} \alpha}{n_e F_e \alpha}.$$

Some simplification of this equation is generally possible because the first term is negligible at typical discharge chamber electron temperatures and energies. In Eq. 21 $V_e$ and $V_0$ are the Bohm$^16$ and neutral atom thermal velocities, $\phi$ and $\phi$ are the transparencies of the grids to ions and neutral atoms and $F_0$, $F_+$ and etc. are the rate factors associated with production of the various ionic species. The primary-to-Maxwellian electron density ratio $(n_e/n_\text{M})$ appearing in Eq. 21 is given by

$$n_e/n_\text{M} = \left[ \frac{0.15 \times e^2 V_e \gamma_\text{p} \gamma_\text{c} \eta_\text{d} \alpha}{\sqrt{V_0} \sqrt{F_0} \gamma_\text{p} \gamma_\text{c} \eta_\text{d} \alpha} \right] \left[ \frac{V_0}{V_e} \right]^{-1/2}.$$

In this equation, the primary electron velocity $(V_e)$ is determined by its energy which is assumed in turn to be equal to the discharge voltage. The discharge chamber volume-to-beam area ratio $(W/A_b)$ is simply the discharge chamber length which may be assumed to be relatively insensitive to barrel area (e.g. $W/A_b = 0.1 + 0.1 [1 - \exp(-10A_b)]$ has been used for the examples presented here). The final expression needed to define the screen grid lifetime constraint is one for the propellant mass flowrate per unit beam area. It is obtained by combining Eqs. 1, 8 and 17.

$$\frac{A_b}{A_p} = \frac{2F_e}{F_+ - \eta_\text{d} \alpha} \frac{S_{\text{co}}}{S_{\text{p}} \gamma_\text{c} \alpha} = \frac{2 F_e}{F_+ - \eta_\text{d} \alpha} \frac{S_{\text{co}}}{S_{\text{p}} \gamma_\text{c} \alpha}.$$

Equations 20 through 23 can be solved for the beam power/beam area/specific impulse surface that defines the screen grid lifetime constraint when an operational constraint is specified and design definitions associated with the chamber (e.g., propellant, discharge voltage, etc.) have been made.
ions and it can be expressed in terms of the energy cost of a beam ion \( (\eta_p) \). Assuming the discharge power does dominate the losses, Eq. 27 can be rewritten as

\[
\eta_p = \frac{V_s}{V_d + \epsilon_d}
\]

and this equation can be combined with those identified above to obtain the expression for thrust-to-total power:

\[
F_J = \frac{I_{\text{sd}}}{\eta_p \cdot V_d + \epsilon_d}
\]

By seeking the propellant utilization that maximizes this equation at each specific impulse, operation at maximum thrust-to-power is realized for each thruster beam area and physical constraint condition.

**RESULTS**

The analysis technique outlined in the preceding section can be used to investigate the effects of a wide variety of design and operational parameters on the power and thrust capabilities of ion thrusters. Because the purpose of this paper is to demonstrate the capability of the methodology involved rather than to draw conclusions based on an exhaustive study conducted using it, one set of Sputter Yield for Accel Grid with the objective of operation above those typically considered to be typical of ion thrusters in general, they do not represent any particular chamber. The rate factors used in the analysis are based on an assumed Maxwellian electron temperature of 5 eV and a primary electron energy, which is consistent with the discharge voltage (30 eV).

Table I. Thruster Parameters Used in Example Study

<table>
<thead>
<tr>
<th>Parameter/Property</th>
<th>Symbol</th>
<th>Value Used</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ion Beam Flatness</td>
<td>( \Phi_f )</td>
<td>0.5</td>
</tr>
<tr>
<td>Ion Current Density Enhancement Factor</td>
<td>( \phi_e )</td>
<td>1.0</td>
</tr>
<tr>
<td>Screen Grid Transparency to Ions</td>
<td>( \phi_s )</td>
<td>0.7</td>
</tr>
<tr>
<td>Grid System Transparency to Neutral Atoms</td>
<td>( \phi_o )</td>
<td>0.16</td>
</tr>
<tr>
<td>Ion Mass (Xenon)</td>
<td>( m_i )</td>
<td>2.2x10^-25 kg</td>
</tr>
<tr>
<td>Net-to-Total Accelerating Voltage Ratio</td>
<td>( R )</td>
<td>0.5</td>
</tr>
<tr>
<td>Beamlet Divergence Thrust Factor</td>
<td>( F_c )</td>
<td>1.0</td>
</tr>
<tr>
<td>Multiply Charged Ion Thrust Factor</td>
<td>( \alpha )</td>
<td>1.0</td>
</tr>
<tr>
<td>Screen Grid Thickness</td>
<td>( t_s )</td>
<td>5x10^-4 m</td>
</tr>
<tr>
<td>Grid Separation to Screen Hole Diameter Ratio</td>
<td>( l_s/d_s )</td>
<td>1.0</td>
</tr>
<tr>
<td>Baseline Plasma Ion Energy Cost</td>
<td>( \epsilon^*_p )</td>
<td>50 eV/1ion</td>
</tr>
<tr>
<td>Extracted Ion Fraction</td>
<td>( f_B )</td>
<td>0.5</td>
</tr>
<tr>
<td>Fraction of Plasma Ions Going to Cathode Potential Surfaces</td>
<td>( f_C )</td>
<td>0.3</td>
</tr>
</tbody>
</table>

If one prescribes a thruster with a beam area of 0.2 m² and calculates the beam power limits for each of the physical constraints described in the preceding section with the objective of operation at maximum thrust-to-power, the curves of Fig. 2 are obtained for the values of the constraints cited in the figure. For each constraint, operation below and to the right of the associated curve assures operation that does not violate the constraint. Hence in the case of Fig. 2 the 600 span-to-gap constraint limits the power that can be extracted up to a specific impulse of -3000 sec and then the

![Fig. 2. Typical Power Constraint Curves - 0.2 m² Beam Area (Span-To-Gap and Intragrid Electric Field Limiting)](image-url)
2 kV/mm electric field constraint becomes limiting. For the particular parameters associated with the other constraints, Fig. 2 indicates none of the other constraints (discharge power, screen grid life, or accel grid life) become limiting at any specific impulse up to 6000 sec. The fact that span-to-gap is limiting at low specific impulses while electric field becomes limiting at higher ones is in qualitative agreement with experimental observations.

If the grids were designed so the electric field limit could be increased to 4 kV/mm and the other constraints were held fixed at the values of Fig. 2, then the data of Fig. 3 are generated. They suggest the 600 span-to-gap limit would prevail to -4000 sec specific impulse and the discharge power per unit beam area limit of 15 kW/m² would become constraining beyond that point. Increasing the electric field limit in this case allowed the beam power at 4000 sec to increase from -15 kW (Fig. 2) to -25 kW (Fig. 3) and at 6000 sec from -27 kW (Fig. 2) to -45 kW (Fig. 3). If, on the other hand, it were necessary to have screen and accel grid lifetimes of 2 x 10⁴ hr then the accelerator grid lifetime would become limiting over the range from about 3500 sec to 4500 sec as the data of Fig. 4 show. In this case the beam power at 4000 sec would be limited by accel grid lifetime considerations to -21 kW.

If the beam power limits imposed by the constraints being considered as functions of both beam area and specific impulse are sought rather than holding beam area constant, then beam power/beam area-specific impulse surfaces like those shown in Fig. 5 are generated. These surfaces define power limits associated with each constraint indicated and they are all plotted on the same scale, namely the one defined in Fig. 5a. Operation is permitted at any point beneath the surface associated with a particular constraint, but not above it. All of these surfaces behave as one would expect with the beam powers being lowest for low beam areas and low specific impulses except the one associated with screen grid lifetime. The high allowable power observed at low specific impulses for the screen life constraint seems unusual. It is a consequence of operation at maximum thrust-to-power which implies a low propellant utilization at low specific impulses (Eq. 29). Low propellant utilizations in turn imply low doubly-to-singly charged ion current densities (Eq. 21) and hence high allowable beam powers (Eq. 20).

When all constraints shown in Fig. 5 are applied and the overall limiting surface is identified, the one shown in Fig. 6 is obtained. As the labels on this surface indicate, the span-to-gap and electric field constraints represent the most restrictive limitations (span-to-gap at low specific impulses and electric field at higher ones) over the beam area range from zero to 1 m².

If one defines a mission along with powerplant and power processor specific mass parameters and then imposes the power limits defined by all of the constraints associated with the data in Fig. 5, payload fractions can be computed as a function of beam area and specific impulse. Figure 7 shows the payload fraction surface computed when the most restrictive of these constraints are applied for a 10⁴ m/sec mission to be accomplished in 0.67 year when the powerplant and power conditioner are characterized by the specific masses and the power conditioner efficiency values cited on the figure. The payload fraction reaches a relatively flat peak at a value of 55 percent when the specific impulse is near 4500 sec for all but the smallest beam areas. The payload fraction peak in Fig. 7 is seen to be very broad, so the thruster could be operated at specific impulses ranging from ~3000 to 6000 sec and deliver about the same payload fraction.

The thrust at which the ion thruster operates can also be computed as a function of beam area and specific impulse by using Eqs. 28 and 29 in conjunction with the most restrictive beam power constraining surface data (Fig. 6). Figure 8 shows how the thrust associated with the constraints defined in Fig. 5 would vary as a function of beam area and specific impulse.

If the electric field constraint is increased to 4 kV/mm, the results of Fig. 3 showed that the discharge power per unit beam area became the power-limiting surface at high specific impulses when the beam area was 0.2 m². The effect of introducing this new electric field constraint for beam areas ranging from zero to 1.0 m² is shown in Fig. 9. Comparison of the data in Figs. 6 and 9 shows that increasing the electric field limit facilitates a substantial increase in beam power at high beam area and specific impulse values (250 kW vs. 150 kW).

If the grid lifetime constraints are tightened by requiring 20,000 hr operating times, then the accel grid lifetime constraint identified in Fig. 10 limits the beam power in the moderate specific impulse-low beam area regime. Away from this region
Fig. 5. Typical Power Constraining Surfaces

Fig. 6. Typical Overall Power Constraining Surface (Span-to-Gap and Intragrid Electric Field Limiting)

Fig. 7. Typical Payload Fraction Surface
The three-dimensional plots shown in Figs. 5 through 10 are useful to illustrate qualitative behavior, but they are difficult to use as a source of quantitative information. Quantitative information can be presented better in the form of an equal beam power contour plot like the one in Fig. 11. This figure, which presents the same data as that in Fig. 10, clearly indicates the beam power limit at any beam area and specific impulse point. It also shows the constraint that is preventing operation at higher power levels at each beam area and specific impulse. Similar figures could, of course, also be generated to show the limiting values of thrust and payload fraction as a function of thruster beam area and specific impulse.

**FUTURE DIRECTIONS**

The intent of the preceding discussion has been 1) to present a methodology and framework within which gross parameters describing ion thruster behavior could be used to predict ion thruster performance limits, 2) to cite references that describe how these gross parameters can be computed, and 3) to suggest how results obtained from the analysis might be presented in a readily understood format. The analysis should, however, not be considered fully developed. The following statements describe changes that might be introduced to improve the analysis.

1) The beamlet divergence (thrust) factor ($F_T$), the grid separation-to-screen hole diameter ratio ($d_s/d_h$) and the net-to-total acceleration voltage ratio ($R$) have all been treated as constants in the cases presented. These quantities are, however, variable and they are related to each other. One could therefore use data like those in Ref. 19 to determine values of $F_T$ for prescribed values of $d_s/d_h$ and $R$ or one could incorporate additional operational objectives that would assure the parameters are selected to maximize a thruster parameter of interest.

2) The screen and accel grid thicknesses ($t_s$ and $t_a$, respectively) have been treated as constants, and depending on the beam geometrical cross section...
it may be that they would be better represented as functions of beam area. For example, a functional relationship between these thicknesses and the beam area based on mechanical deformation considerations might be desirable.

3) Although some variation in discharge chamber plasma properties has been allowed in the development of the screen life constraint, more can be done in modeling the other constraints to reflect the effects of changes in Maxwellian electron temperature, primary and Maxwellian electron densities, the baseline plasma ion energy cost (e_0) and the doubly-charged ion thrust factor (a) induced by changes in propellant utilization and discharge voltage. It is noted that the physically based models needed to do this are available.

4) The grid spacing has been assumed constant across the entire intragrid region. The effects of variable spacing induced by grid thermal distortion and electric field induced deflection forces may cause this spacing to change as a function of location on the grids. This in turn will influence the ion extraction and electrical breakdown capabilities of the grids.

Finally, it is noted that many of the parameters needed to model the plasma discharge and ion extraction phenomena involved in this analysis can be computed from basic principles. The noteworthy exception to this is the primary electron containment factor, 1. It can be inferred from discharge chamber tests, but a model that can be used to calculate it for a discharge chamber having prescribed dimensions and magnetic field characteristics is needed. Additional work may also be needed to describe more accurately the energy of primary electrons extracted from a hollow cathode as a function of discharge voltage.

CONCLUSIONS

A methodology that can be used to determine the maximum power level at which an ion thruster can be operated and a framework within which the resultant data can be presented has been developed. Physical constraints associated with the allowable grid span-to-gap ratio, the intragrid electric field, the discharge power per unit beam area and the screen and accel grid lifetimes have been identified as power (or thrust) limiting and relationships that quantify each of the constraints have been presented. Log is exercised for a thruster operating on xenon at propellant utilization efficiencies that induce maximum thrust-to-power with constraints of 600 span-to-gap ratio, 2 kV/m, 15 kV/m^2 discharge power per unit beam area and 10^4 hr screen and accel grid lifetime requirements, the span-to-gap constraint is shown to be limiting at low specific impulses and the electric field is shown to be limiting at higher ones. If the electric field limit is increased to 4 kV/m, the discharge power becomes limiting at high specific impulses and if the grid lifetime requirement is increased to 2 x 10^4 hr then accel grid erosion can become limiting at intermediate specific impulses. Although the input data have not been selected to result as predicted in the analysis, it can be compared to experimental observations, the general trends appear to be consistent with generally observed experimental trends.

REFERENCES


