Monte Carlo Simulation of Neutral Xenon Flows
Of Electric Propulsion Devices

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Abstract

Numerical simulations of neutral xenon flow in three different electric propulsion configurations are presented. Flows through an ion thruster, a plasma contactor, and a Hall thruster are considered. The computations are performed using a Monte Carlo method that can simulate both collision and plasma phenomena. The ion thruster configuration chosen for study is the UK-10 engine. Comparisons of the simulations are made with a simple analytical model that has been used in previous computations of back flow from ion thrusters. Both sets of theoretical results are compared with number density measurements. The Monte Carlo simulations provide closer agreement with the experimental data and the analytical model is found to under predict density in the back flow plume region. The Monte Carlo simulation of the plasma contactor plume also compares well with experimental measurements. For the Hall thruster, the simulations reveal some interesting behavior in the annular anode chamber. Comparison with a measured data point for velocity appears to indicate a discrepancy in the experiment.

Introduction

Xenon is the propellant of choice for many electric propulsion devices. For example, use of xenon ion thrusters is now planned on several spacecraft missions including the New Millennium program of NASA, the HS-601 and HS-702 satellites of Hughes, and the AKEMIS spacecraft of ESA. Russian Hall thrusters using xenon have been flying for many years. This propellant is also being considered for use in resisto-jets [1] and pulsed plasma thrusters [2]. While increasing use of electric propulsion in space indicates an acceptance of the reliability and performance of this technology, there is a continued need for detailed analysis of these systems for two specific reasons. First, the thrust efficiencies of electric propulsion devices is low (e.g. 50% for an ion thruster). Improvement in this performance is most likely attained through a comprehensive understanding of the operation of the device. Second, there is a concern over the interaction between the spacecraft and the plume flow field generated by the thruster. For ion thrusters, the impact of heavy metallic ions sputtered from the acceleration grids is of particular concern. These ion impacts are most problematic in the plume backflow region behind the thruster exit plane. The ions are accelerated into this region by the electric fields associated with the charge exchange plasma.

The present study considers numerical simulation of xenon plumes from electric propulsion devices. As explained above, the main issue in such plumes is the charge exchange phenomenon in which a high energy ion collides with a low energy neutral atom to produce a low energy ion and a high energy atom. The low energy ion has the possibility to diffuse into the thruster back flow region, creating electric fields that ultimately attract the heavy metallic ions. Any computation that aims to model these phenomena accurately must simulate both the xenon ions and the xenon atoms. The specific focus of the work presented here concentrates on the simulation of the xenon atoms. A companion paper considers the effects of the ions in an ion thruster [3].

In this paper, a description is first made of the computer code and physical models employed for the numerical simulations. Results of neutral xenon flow computations are then presented for three different configurations. First, flow is computed for the UK-10 ion thruster. Comparison of the simulated results is made with a simple analytical model and with experimental measurements. Next, results for a plasma contactor geometry are provided and again comparison with measured data is provided. Finally, simulation results are presented for neutral xenon flow through a Hall thruster geometry.

Numerical Method

In plumes from many electric propulsion devices, both collision and plasma effects are important. A
computer code has been developed that simulates these phenomena using a combination of two different particle methods. The collisions are treated using the direct simulation Monte Carlo method (DSMC) [4]. In this technique, particles move through physical space undergoing collisions with other particles and with solid surfaces. A computational grid is employed to group together particles that are likely to collide, and for evaluating macroscopic flow properties. A novel implementation of the DSMC technique has been developed [5] for efficient numerical performance on a range of computer platforms. The code may be executed on scalar work-stations and parallel supercomputers. The DSMC code is called MONACO [5] and has been successfully applied to low density problems in spacecraft propulsion, hypersonics, and plasma processing of materials. Plasma effects are treated using the Particle In Cell method (PIC) [6]. This method uses particles to determine the charge density. The charge density defines the electrostatic field forces that affect the trajectories of the charged particles. Details of the implementation of this hybrid computer code are provided in Ref. 3.

In the studies described here, only the DSMC portion of MONACO is employed to simulate a number of different neutral xenon flows. One of the strengths of MONACO lies in its use of unstructured grids that provide great flexibility in terms of simulating geometric complexity. In all simulations performed here, the variable hard sphere (VHS) collision model of Bird is employed [4]. For neutral xenon, the model parameters are: reference collision diameter, \( d_{ref} = 5.74 \times 10^{-10} \text{ m} \), and viscosity temperature exponent, \( \omega = 0.62 \).

**Results**

The flow of xenon atoms is computed for three different electric propulsion configurations. Specifically, these are: (1) the UK-10 ion thruster; (2) a plasma contactor; and (3) a Hall thruster. The motivation for studying the neutral flow only is to demonstrate the accuracy of the DSMC-PIC code for simulating the behavior of the atoms in the absence of plasma effects. The importance of accurate computation of the neutral flow field should not be underestimated since it participates directly in the creation of any charge exchange plasma.

**1. Ion Thruster**

The specific reason for considering the UK-10 thruster is the availability of experimental measurements by Crofton [7] of the flow of neutral xenon atoms through the device with the current turned off. The simulations presented here are begun at the thruster exit plane using input conditions of \( \dot{n}_0 = 0.61 \text{ mg/s} \), a Mach number of 1, and a stagnation temperature of 295 K. The plume is assumed to expand into a vacuum. An important issue in simulating the UK-10 thruster concerns the interaction between the neutral flow and the dished grids employed in this device. In the results presented here, it is assumed that the grids have no effect on the neutral flow and that the xenon atoms exit the thruster with a mean radial velocity component of zero. A second issue concerns the distribution of the atoms across the thruster exit plane. In the results shown here, a uniform density profile is employed. The calculations using MONACO employ 11,000 cells and 100,000 particles. The flow domain extends 1 m along the axis from the thruster exit and 1 m radially. The simulation is performed on an IBM work-station and requires 3 hours execution time.

In previous PIC simulations of ion thruster plumes [8], the neutral xenon atoms were not treated directly in the computation. Instead, the number density of atoms was approximated using the following analytical expression:

\[
\rho(R, \theta) = a n_o \left(1 - \left[1 + \left(r_T/R\right)^2\right]^{-3/2}\right) \cos(\theta) \tag{1}
\]

where \( r \) and \( z \) are the radial and axial distances from the point on the centerline at the thruster exit, \( r_T \) is the thruster exit radius, \( R = \sqrt{r^2 + (z + r_T)^2} \), \( \theta = \tan^{-1}[r/(z + r_T)] \), \( a \) is a correction factor, and \( n_o \) is the number density at the thruster exit. This expression was used to compute a source term of charge exchange ions that led to plume backflow. One of the goals of the present study is to assess the effectiveness of this expression for the UK-10 thruster.

In Fig. 1, contours of number density for the flow computed using the Monte Carlo code (upper half) and with Eq. (1) (lower half) are compared. Qualitatively, both solutions exhibit the expected behavior for a low-density plume expansion. At first sight it appears as though there is very good agreement between the two sets of results. This is certainly true far along the axis where the density decays with the inverse square of distance from the thruster exit. However, close to the thruster exit at large radial distance there are significant differences.

Comparison of the Monte Carlo and analytical results for number density with the experimental data of Crofton [7] along the plume axis and radially at distances of 4.5 cm and 15 cm from the exit plane are shown in Figs. 2, 3, and 4 respectively. The experimental data were obtained using a non-intrusive, two-photon, laser-induced fluorescence technique that presents calibration difficulties.
Therefore, the comparisons can only be made for normalized data. For each of the three data sets (experiment, Monte Carlo, and analytical model) the data are normalized using the value at the thruster exit plane on the plume axis. All of the experimental data shown here has been corrected for the finite pressure of the vacuum chamber [7].

Along the plume axis, good agreement between Monte Carlo prediction and measurement is obtained throughout. The simple model shows a significant under prediction of density close to the thruster exit. At large distances from the thruster, the analytical model approaches the Monte Carlo results. In the radial profile at 4.5 cm from the thruster, good agreement is again obtained between the Monte Carlo simulation and the experimental data. As expected from Fig. 3, the simple model under predicts the density on the axis by about 50% in comparison to the measured data. In addition, the model predicts a flatter profile for the plume shape. At 15 cm from the thruster, all three profiles are very flat. The Monte Carlo computations continue to provide good agreement with the experimental data. The analytical model continues to show an error of about 50%.

To consider in detail the importance of neutral xenon modeling for simulation of the charge exchange plasma, the ratio of the two solutions (Monte Carlo divided by Eq. (1)) is shown in Fig. 5. Note that when current is applied to the thruster, the main ion beam of the plume is confined to a cylinder of radius 5 cm about the plume axis. The contours in Fig. 5 indicate that there is at worst only a 50% disagreement between the Monte Carlo and model results inside this region. However, close to the thruster exit plane, just outside the main beam area, there are orders of magnitude differences between the two solutions. In particular, the analytical model under predicts the neutral xenon number density in this region.

It is difficult to assess definitively the effect on predicted charge exchange plasma that may occur as a result of using the simple analytical model. The volumetric production rate of charge exchange ions may be written:

\[ \nu_{\text{CEX}} = n_i V_i \sigma_{\text{CEX}}(V_i) \]  

(2)

where \( n_i \) is the ion number density, \( V_i \) is the ion velocity (much greater than neutral xenon velocity), and \( \sigma_{\text{CEX}} \) is the charge exchange cross-section that is a function of ion velocity. From Eq. (2), it is clear that most of the production of charge exchange ions will occur in the main beam area, and this region is quite well represented by the model. However, the amount of charge exchange ions that actually arrive in the backflow region is extremely small so that the inaccuracy of the simple model in this region may be significant.

2. Plasma Contactor

Neutral xenon measurements in the plume of flow through a plasma contactor configuration were reported by Williams and Wilbur [9]. The present computation of this flow is begun at the exit plane of the cathode. A portion of the grid used for the Monte Carlo computations is shown in Fig. 6 indicating the positions of the cathode and anode. The cathode has an exit diameter of 0.76 mm and is assumed to be at a temperature of 1,300 K. Neutral xenon exits this orifice at a flow rate of \( 4 \times 10^{-7} \) kg/s with sonic conditions assumed. The anode is located 2 mm downstream of the cathode exit, has a total diameter of 120 mm and an orifice diameter of 5 mm. The anode temperature is assumed to be 300 K. The cathode and anode are coaxial. A back pressure of \( 3.1 \times 10^{-4} \) torr (corresponding to a number density of \( 10^{17} \) m\(^{-3} \) at 300 K) is assumed for the vacuum chamber. The entire computational domain is shown in Fig. 7. Here, the benefit of being able to employ a general unstructured grid format in MONACO is illustrated. Clustering of cells is achieved in regions of high density through a combination of triangular and quadrilateral cells.

Contours of number density in m\(^{-3} \) for the entire flow field are shown in Fig. 8. Again, the expected trend for an orifice expansion is observed. Note in the far field that the number densities approach the vacuum chamber background level. In Fig. 9, contours of translational temperature in degrees Kelvin are shown. Here the influence on the expansion of the anode and the finite back pressure may be seen. Close to the anode, the flow is heated to 300 K. Moving away from the orifice, the expanding flow first shows decreasing temperature. However, as the particles of the background gas interact with the expanding plume, the temperature is again raised. Note that beyond very small distances from the cathode that the translational temperatures along the plume axis are significantly lower than 300 K.

In Fig. 10, comparison is made between the experimental measurements of Ref. 9 and the Monte Carlo computations for number density along the plume axis. Here, the origin is taken to be the plane of the anode. The data in Ref. 9 are reported as number density values although pressure was measured. The conversion from pressure to density employed the perfect gas law and assumed the temperature to be constant at 300 K. In Fig. 10, two different sets of Monte Carlo results are shown. The first ("uncorrected") is the number density actually computed by
MONACO. These values are significantly higher than the experimental data. From Fig. 9, however, it is clear that the translational temperatures are not constant at 300 K for the region where the measurements were conducted. Hence, a second Monte Carlo solution ("corrected") is obtained using the same procedure employed in Ref. 9. The pressure computed by MONACO is used to compute a number density using the perfect gas law and by assuming the translational temperature to be 300 K. This procedure leads to a profile that is in excellent agreement with the experimental measurements.

3. Hall Thruster

A laboratory scale Hall thruster has been designed and built at Stanford University for the purposes of developing diagnostic techniques [10]. In Ref. 10, a laser induced fluorescence technique was developed for measuring the velocity of neutral xenon atoms. Experimental data were reported for both cold flow (no current) and full operational conditions. The geometry of the Stanford Hall thruster is indicated in Fig. 11 in which the grid employed for the present Monte Carlo computations is shown. Xenon is injected through 32 holes of diameter 0.5 mm with each hole centered at a radial distance of 4 cm from the axis. This flow passes through a small annular chamber before expanding out into the vacuum chamber. The upper and lower surfaces of this chamber are the south and north magnetic poles, respectively. The left hand side of the chamber contains the propellant feed system and also acts as the anode. A cathode is placed above the thruster and operates with a flow rate that is 10% of that through the anode.

The cold-flow case is computed using a mass flow rate of 2.9 mg/s and assuming the flow at the injection orifice is choked. The 32 discrete orifices are modeled by a continuous annulus. All surfaces are assumed to have a temperature of 295 K. The flow from the cathode is neglected. The plume expansion is assumed to occur into perfect vacuum.

The grid shown in Fig. 11 is adapted everywhere so that cell sizes are of the order of one mean free path. Inside the first chamber, the Knudsen number (ratio of mean free path to chamber diameter) is about 0.01 placing the flow in the near continuum regime. This flow is characterized by a relatively high collision rate requiring small computational cells. In the plume expansion, the number density falls by many orders of magnitude leading to almost collisionless flow. This allows use of much larger cells.

In Fig. 12, contours of Mach number computed inside the annular anode chamber are shown. The flow first expands rapidly to a peak Mach number of about 1.25. Then, strong viscous interaction between the fluid and the walls leads to the generation of a large boundary layer that causes deceleration of the flow. The flow then re-accelerates as the exit plane is approached to reach the sonic condition. Beyond the exit plane the flow is supersonic.

Contours of number density in m\(^{-3}\) are shown in Fig. 13 and indicate that the plume expands rapidly away from the thruster exit. In Fig. 14, contours of computed velocity are shown. The experimental technique described in Ref. 10 provides a measurement of the velocity of neutral xenon. For the cold-flow condition, the axial velocity is measured to be 100 m/s at a point in the center of the anode chamber annulus 5 mm downstream of the exit plane. The Monte Carlo computation predicts an axial velocity of 185 m/s at this point in the flow field. The experimental datum is surprisingly low and indicates subsonic flow. It is likely that the experimental measurement has been affected by the relatively high chamber pressure in the facility of 3 \(\times\) 10\(^{-4}\) torr which corresponds to a number density of 10\(^{10}\) m\(^{-3}\) at 295 K. As seen in Fig. 13, this density is reached at a small distance from the thruster exit.

Summary

The goal of this study was to assess the ability to accurately simulate neutral xenon flows. The motivation for the investigation is provided by the widespread use of xenon in a variety of electric propulsion devices combined with the important role played by the neutral atoms in forming charge exchange plasma. To meet this goal, numerical simulations of neutral xenon flow in three different electric propulsion configurations were performed. Specifically, flows through an ion thruster, a plasma contactor, and a Hall thruster were considered. The computations were performed using a Monte Carlo method that can simulate both collision and plasma phenomena. For the UK-10 ion thruster, the Monte Carlo computations were used to assess the accuracy of a simple analytical model employed in previous studies of ion thruster plumes to approximate the distribution of neutral atoms. While reasonable agreement was obtained between the two solutions close to the plume axis, the model under predicted density by orders of magnitude in the back flow plume region. Both sets of theoretical results were compared with number density measurements. The Monte Carlo simulations provided excellent agreement with the experimental data. Excellent agreement of the Monte Carlo predictions with experimental data was also obtained in the plasma contactor plume. For the Hall thruster, the simulations indicated significant viscous
interaction inside the annular anode chamber. Comparison of the computation with a single experimental data point for velocity indicated significant disagreement. The experimental value implies subsonic flow. This would not be expected in a plume expansion and suggests some interference of the flow in the experiment. In conclusion, it has been shown that the Monte Carlo computer code MONACO can provide accurate numerical simulations of neutral xenon flow in a variety of different realistic electric propulsion configurations.

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References

Figure 3: Radial variation in normalized xenon density at a distance of 4.5 cm from the thruster exit plane.

Figure 5: Ratio of number densities: Monte Carlo prediction divided by analytical model.

Figure 4: Radial variation in normalized xenon density at a distance of 15 cm from the thruster exit plane.

Figure 6: Close-up view of computational grid showing geometry of cathode and anode for plasma contactor.
Figure 7: Grid employed for Monte Carlo computation of plasma contactor plume illustrating mixture of quadrilateral and triangular cells.

Figure 8: Contours of number density for the plasma contactor plume.

Figure 9: Contours of translational temperature for the plasma contactor plume.

Figure 10: Density along the axis of the plasma contactor plume.
Figure 11: Unstructured grid employed for simulation of neutral flow through the Stanford Hall thruster.

Figure 12: Computed Mach number contours of neutral flow inside the Stanford Hall thruster.

Figure 13: Computed number density contours of neutral flow in the plume of the Stanford Hall thruster.

Figure 14: Computed velocity contours of neutral flow in the plume of the Stanford Hall thruster.