Electromagnetically Driven Fusion Propulsion

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John Slough1
University of Washington, Plasma Dynamics Laboratory, Redmond, WA, 98052, USA

and

Anthony Pancotti2, David Kirtley3, George Votroubek4
MSNW LLC, Redmond, WA, 98052

Abstract: The Fusion Driven rocket (FDR) represents a revolutionary approach to fusion propulsion where the fusion plasma releases its energy directly into the propellant, not requiring conversion to electricity. It employs a solid lithium-based propellant that requires no significant tankage mass. Several low-mass, magnetically-driven metallic liners are inductively driven to converge radially and axially to form a thick blanket surrounding the target plasmoid compressing the plasmoid to fusion ignition conditions. Virtually all of the radiant, neutron and particle energy from the plasma is absorbed by the encapsulating, thick metal blanket. This combined with a large buffer region of high magnetic field isolate the spacecraft from the energetic plasma created by the fusion event. The current effort is focused on achieving three key criteria needed for further technological development of the Fusion Driven Rocket: (1) understanding the physics of the FDR through actual liner driven fusion experiments and validating models for predictive analysis (2) an in-depth analysis of the rocket design and spacecraft integration as well as (3) a detailed study of the mission architectures enabled by the FDR. Review of the progress on all three efforts is presented.

Nomenclature

\[
\begin{array}{ll}
A &= \text{cross sectional area of liner} \\
A_s &= \text{surface area of liner} \\
\beta &= \text{ratio of plasma pressure to magnetic pressure} \\
B &= \text{magnetic field} \\
B_e &= \text{external magnetic field} \\
B_{in} &= \text{internal magnetic field} \\
B_0 &= \text{internal field at peak compression} \\
C &= \text{capacitance} \\
\delta &= \text{liner thickness}
\end{array}
\]

1 Res. Assoc. Prof., Aeronautics and Astronautics, sloughj@UW.edu
2 Senior Scientist, pancotti@msnwllc.com
3 Dir. Propulsion Research, dkirtley@msnwllc.com
4 Senior Scientist, gvotho@msnwllc.com
\( \delta_{\text{gap}} \) = initial gap between driver coil and liner
\( \varepsilon \) = FRC elongation ratio (\( l_0/2r_s \))
\( E_B \) = magnetic field energy
\( E_{\text{fus}} \) = fusion energy
\( E_L \) = liner kinetic energy
\( F \) = force on liner
\( \text{FRC} \) = field reversed configuration
\( G_{\text{Al}} \) = action constant for aluminum
\( g_m \) = action constant for material \( m \)
\( G \) = fusion gain
\( I \) = current
\( I_{\text{sp}} \) = specific Impulse
\( L \) = inductance
\( L_{\text{gap}} \) = inductance of coil-liner gap
\( l_0 \) = FRC length at peak compression
\( l_s \) = FRC length
\( M_L \) = liner mass
\( n_0 \) = plasma density at peak compression
\( \mu_0 \) = free space permeability
\( P_B \) = magnetic pressure
\( \rho_m \) = density of material \( m \)
\( r \) = radius variable
\( r_c \) = coil radius
\( r_0 \) = liner radius at peak compression
\( r_s \) = FRC separatrix radius
\( R \) = object radius
\( r_L \) = liner radius
\( \Delta r \) = liner radial displacement from magnetic force
\( \langle \sigma v \rangle \) = D-T fusion cross section
\( \Delta t \) = time step
\( T_e \) = electron temperature in eV
\( T_i \) = ion temperature in eV
\( T_0 \) = plasma total temperature at peak compression
\( \tau_D \) = liner dwell time
\( v_L \) = liner velocity
\( v_{\text{max}} \) = maximum liner velocity
\( V_C \) = initial voltage on capacitors
\( w \) = liner width

1. Introduction

The future of manned space exploration and development of space depends critically on the creation of a dramatically more efficient propulsion system for in-space transportation. This has been recognized for many years. Not as well recognized is the need for high power, high \( I_{\text{sp}} \) propulsion in Low Earth Orbit (LEO) as it relates to several unmanned orbital maneuvers that are quite costly or not feasible with current chemical propulsion rockets. Of particular value to both military and commercial interests would be a high power orbital tug that can shuttle numerous payloads of several metric tons (MT) from LEO to GEO.

A very persuasive reason for investigating the applicability of nuclear power for these missions is the vast energy density gain of nuclear fuel when compared to chemical combustion energy. The combustion of hydrogen and oxygen has an energy release of 13 MJ/kg, whereas the fission of \(^{235}\text{U}\) yields approximately \(8 \times 10^7\) MJ/kg and the fusion of deuterium and tritium has a \(3.6 \times 10^8\) MJ/kg yield. So far, the use of fission energy represents the nearest term application of nuclear power for propulsion. Several fission based propulsion schemes have been proposed for in-space transportation, including pulsed nuclear explosions and the Nuclear Thermal Rocket\(^1\) (NTR). In the NTR a
cooling fluid or propellant is passed through a core of material that has been heated by fission. This makes the NTR effectively a heated gas rocket. With the present limitations of materials, NTR gas temperatures cannot exceed chemical propulsion gas temperatures. The use of hydrogen provides for an increase in Isp to 900 s. With $\Delta V \sim 9$ km/sec the propellant mass is reduced by an order of magnitude for a given spacecraft mass. Unfortunately, this is considerably offset by increased spacecraft mass (payload, structure, shielding, tankage etc.). A significant mass is required for the low mass density propellant ($H_2$) as the specific gravity of liquid hydrogen is around 0.07, compared to 0.95 for an $O_2-H_2$ chemical engine. The net result then is a propulsion system that is better than chemical, but not enough to really be a “game changer”. Proposed Nuclear Electric Propulsion (NEP) systems employ high Isp thrusters like the ion and Hall thrusters which solves the propellant Isp issue. The problem for NEP is the inherent inefficiency of the electrical power generation. Shedding the excess reactor heat requires an enormous radiator mass. The large reactor and power conversion masses just add to this problem making for too low a specific power (ratio of jet power to system mass) for rapid space transport.

Invoking nuclear fusion for space propulsion, at least as it has been envisioned up till now, does not significantly alter this picture as it has been developed primarily as an alternate source for electrical grid power. This endeavor is far from completion, and even if nuclear fusion were to be eventually developed for terrestrial power generation, the resulting power plant would be unlikely to have any role in space propulsion for all the same reasons that trouble NEP - but worse. Past efforts in this regard have all come to be dismissed, and rightfully so, primarily for the following two reasons. The first has been alluded to already. The propulsion system is reactor based. The straightforward application of a reactor-based fusion-electric system creates a colossal mass and heat rejection problem for space application. In a detailed analysis for the most compact tokamak concept, the spherical torus, spacecraft masses of 4000 metric tons (mt) were projected. The maximum launch mass would need to be less than 150 MT if current chemical rockets are used for launch to LEO. The second is the use of the fusion plasma and/or the fusion products as propellant. Due to the resultant high exhaust velocities, the enormous mismatch from the appropriate exhaust velocity leaves the spacecraft with either insufficient thrust or enormous power requirements. Exotic fuels ($^3$He) or fuels with marginal fusion reaction efficiencies (e.g. P-$^{11}$B) with large circulating powers are also required.

If one were to imagine the optimal solution to this predicament, it would be a fusion propulsion system where (1) the power source releases its energy directly into the propellant, not requiring conversion to electricity. (2) It would employ a solid propellant that would require no significant tankage mass. (3) The propellant is readily heated and accelerated to high exhaust velocity ($> 20$ km/s), and where the propellant (4) has no significant physical interaction with the spacecraft thereby limiting thermal heat load, spacecraft damage, and radiator mass. The Fusion Driven rocket to be detailed in this paper represents an attempt to incorporate all four of these attributes, and in so doing, lead to a practical propulsion system that is capable of taking full advantage of the promise that fusion energy represents.

II. Fusion Driven Rocket

In this section the physics and method for achieving the compressional heating required to reach fusion gain conditions based on the compression of a Field Reversed Configuration plasmoid (FRC) is elucidated. In brief, an inductive technique is employed to accelerate an array of thin, predominantly lithium metal bands radially inward to create a three dimensional compression of the target FRC in a manner compatible with application in space.

A. Background

As first demonstrated at Trinity site (fission) and then at Eniwetok Atoll (fusion), the ignition of nuclear fuels have certainly confirmed the ability to produce copious energy yields from nuclear energy, dwarfing that of the Atlas V by many orders of magnitude. The challenge is how to have the release of nuclear energy occur in such a manner as to be a suitable match to that desired for manned planetary transportation or high power orbital maneuvers: multi-megawatt jet power, low specific mass ($\sim 1$ kg/kW) at high Isp ($> 2,000$ s). It would appear that for at least nuclear fission, there is no real possibility of scaling down to an appropriately low yield as a certain critical mass (scale) is required to achieve the supercritical chain reaction needed for high energy gain. Fission nuclear pulse propulsion then, such as that envisioned in the Orion project, ends up with a thrust in the millions of megatons which would only be suitable for spacecraft on the order of 107 million MT - the mass of over 100 aircraft carriers!
Fortunately, the critical massSCALE for fusion ignition can be much smaller. The criteria to achieve D-T fusion ignition, at a nominal fuel (plasma) temperature of 10 keV, is the attainment of a density-radius product of $\rho \cdot R \sim 0.1 \text{g/cm}^2$. This can be accomplished with a three dimensional compression of a spherical cryogenic fuel pellet of millimeter scale. Here it is assumed that the inertia of the small pellet is sufficient to confine the plasma long enough for the burn to propagate through the pellet and thereby produce an energy gain $G \sim 200$ or more ($G = \text{fusion energy/initial plasma energy}$). This Inertial Confinement Fusion (ICF) approach has been actively pursued for decades as it represents essentially a nano-scale version of a fusion explosive device. Because of the small scale and tiny masses, the energy delivery system required to heat the pellet to fusion temperature must be capable of doing so on the nanosecond timescale. It appeared that the most promising solution to accomplish this is with a large array of high power pulsed lasers focused down on to the D-T pellet. While the anticipated energy yield is in the range appropriate for propulsion ($E \sim 20$-100 MJ), the scale and mass of the driver (lasers and power supplies) is not, as it requires an aerial photograph to image the full system.

There have been however three breakthrough realizations in the last several years that have provided the keys to achieving inertial fusion at the right scale in an efficient and appropriate manner for space propulsion. They primarily concern the enhanced confinement provided by significant magnetization of the target plasma which considerably eases the compressive requirements for achieving fusion gain and even fusion ignition. This new approach to fusion is aptly referred to as Magneto-Inertial Fusion (MIF), and will now be briefly described.

B. Magneto Inertial Fusion

The notion of using means other than an array of high power lasers to compress the target to fusion conditions goes back as far as the 1950’s. Heavy ions and metal shells (liners) were two of the most promising. They all had in common the basic approach of ICF, i.e. the outer shell or liner is driven directly or indirectly inward compressing the inner target to fusion conditions. Regardless of method, this compression must be uniform, intense and accomplished with great precision resulting in large, high voltage and expensive driver systems. By the mid-nineties it was realized that the presence of a large magnetic field in the target would substantially suppress the thermal transport, and thus lower the imploding power needed to compress the target to fusion conditions. With more time before the target plasma thermal energy was dissipated, a much more massive confining shell could be employed for direct compression, with the dwell time of the confining (metal) shell now providing for a much longer fusion burn time. The liner does not need to be propelled inward by ablation but could be driven by explosives or even magnetic fields. In a seminal paper by Drake et al. it was shown that with a fully three dimensional imploding shell on to the magnetized target, fusion gain could be achieved on a small scale with sub-megajoule liner (shell) kinetic energy. There was no known way to accomplish this at that time, but it was feasible at least in theory.

The second major theoretical result was obtained by Basko et al. who showed that for a sufficiently magnetized target plasma, fusion ignition would occur even when the restrictive condition that $p \cdot R > 0.1 \text{g/cm}^2$ was far from being met. Ignition was now possible as long as the magnetic field-radius product, $B \cdot R > 60 \text{T-cm}$. Thus fusion ignition could be obtained for MIF targets with much lower compression than required for ICF as Fig. 1 indicates. The final critical element to enable fusion energy to be utilized for space propulsion was a practical method to directly channel the fusion energy into thrust at the appropriate Isp. It is believed that such a method has been determined that is supported by both theory and experiment. A description of the operating principles of the Fusion Driven Rocket will now be given.

Figure 1. The BR form of the Lindle-Widner diagram. Ignition curves for different product BR (taken from Ref. 4). When the BR parameter exceeds the threshold value, the $dT/dt > 0$ region extends to infinitely small $p \cdot R$ and ignition becomes possible at any $p \cdot R$. 

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C. Fusion Propulsion Based on Inductively-Driven Metal Shell Compression of a Magnetized Plasmoid

It was clear that fusion ignition conditions could be achieved at small scale by transferring the kinetic energy of a significantly more massive metal shell than the target plasma to compress it to high density and temperature. The question now becomes: (1) how to do this without invoking a massive and complex driver (2) how to do it in a manner that is efficient and capable of repetitive operation (3) how to create a suitable magnetized plasma target, and (4) how to transfer the fusion energy into a suitably directed propellant at optimal exhaust velocities and powers for the missions mentioned earlier.

The key to answering all four “hows” is based on previous experimental work employing inductively driven liners to obtain megabar magnetic pressures\(^5,6\), and magnetic compression of Field Reversed Configuration (FRC) plasmoids to fusion conditions\(^7,9\). A logical extension based on these results leads to a propulsion method that utilizes these metal shells to not only achieve fusion conditions, but then to become the propellant as well. The basic scheme for Fusion Driven Rocket (FDR) is illustrated and described in Fig. 2. The two most critical matters in meeting challenges (1) and (2) for MIF, and all ICF concepts for that matter, is driver efficiency and “stand-off” – the ability to isolate and protect driver and thruster from the resultant fusion energy release. By employing metal shells for compression, it is possible to produce the desired convergent motion inductively by inserting the metal shells along the inner surface of cylindrical or conically tapered coils. Both stand-off and energy efficiency issues are solved by this arrangement. The metal shell can be positioned up to a meter or more from the target implosion site with the coil driver both physically and electrically isolated from the shell. The driver efficiency can be quite high as the coil driver is typically the inductive element of a simple oscillating circuit where resistive circuit losses are a small fraction of the energy transferred. Even though there is essentially no magnetic field within the liners initially, there is enough flux leakage during the inward acceleration that at peak compression the axial magnetic field that is trapped inside the now greatly thickened wall can reach as high as 600 T\(^6\). As will be seen this field is considerably higher than that

Figure 2. Schematic of the inductively driven metal propellant compression of an FRC plasmoid for propulsion. (a) Thin hoops of metal are driven at the proper angle and speed for convergence onto target plasmoid at thruster throat. Target FRC plasmoid is created and injected into thruster chamber. (b) Target FRC is confined by axial magnetic field from shell driver coils as it translates through chamber eventually stagnating at the thruster throat. (c) Converging shell segments form fusion blanket compressing target FRC plasmoid to fusion conditions. (d) Vaporized and ionized by fusion neutrons and alphas, the plasma blanket expands against the divergent magnetic field resulting in the direct generation of electricity from and the back emf and a directed flow of the metal plasma out of the magnetic nozzle.
required for the compression of an FRC to achieve ignition and substantial fusion gain.

The next challenge to be considered is the magnetized plasma to be used as the fusion target. Spaced-based fusion demands a much lower system mass. The lowest mass system by which fusion can be achieved, and the one to be employed here, is based on the very compact, high energy density FRC (see Fig. 3). It is of paramount advantage to employ a closed field line plasma that has intrinsically high $\beta$ (plasma/magnetic pressure ratio), and that can be readily translated and compressed, for the primary target plasma for MIF. Of all fusion reactor embodiments, only the FRC plasmoid has the linear geometry, and sufficient closed field confinement required for MIF fusion at high energy density. Most importantly, the FRC has already demonstrated both translatability over large distances as well as the confinement scaling with size and density required to assure sufficient lifetime to survive the timescale required for compression. FRCs can, and have been generated with enough internal flux to easily satisfy the B*R ignition criteria at peak compression. At a nominal liner converging speed of 3 km/s, a 0.2 m radius FRC typical of operation on the LSX FRC device would be fully compressed in 67 $\mu$s which is only a fraction of the lifetime that was observed for these FRCs (~ 1 msec).

Finally, to complete the fourth challenge, a straightforward way to convert the fusion energy into propulsive energy must be devised. It is accomplished by employing an inductively driven thin metal liner to compress the magnetized plasma. As the radial and axial compression proceeds, this liner coalesces to form a thick ($r > 5$ cm) shell that acts as a fusion blanket that absorbs a large fraction of the fusion energy as well as the radiated plasma energy during the brief fusion burn time. This superheated blanket material is subsequently ionized and rapidly expands inside the divergent magnetic field of the nozzle. Here the thermal energy of the plasma is converted into directed propulsive thrust much like in a conventional nozzle but with the crucial difference being that the isolation provided by the magnetic field protects the chamber wall from bombardment by the energetic plasma ions. It would be possible to also derive the electrical energy required for the driver system from the back emf experienced by the conical magnetic field coil circuit via flux compression. It was found however that the power required for recharging the energy storage modules for the metal liner driver coils could readily be obtained from conventional solar electric power. For very rapid, high power missions, the flux compressor/generator

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**Figure 3.** Elongated Field Reversed Configuration (FRC) Equilibrium Magnetic Field lines and Pressure Contours. $R$ is the radius to the FRC magnetic null, $L_s$ and $r_s$ are the FRC separatrix length and radius respectively.

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**Figure 4.** AEDS calculation of the 3D behavior of three 40 cm radius, 5 cm wide, 0.2 mm thick Aluminum liners converging onto a stationary test target. The scale of the ellipsoid target (1x3.5 cm) is that anticipated for an initially 20 cm radius FRC compressed to 1 megabar energy density (410 T field).
option could be adopted. For a near-term manned Mars mission, solar electric requires the least technology
development, lowest cost, and is already at the highest TRL level.

D. Physics of the Fusion Driven Rocket

The analysis of the liner implosion was carried out for both the subscale validation experiment now being
performed at the University of Washington (UW), as well as what would be required for a full scale FDR prototype.
For the purposes of the analysis given here, a very conservative estimate of the liner kinetic energy that could be
achieved is based on both modeling and what other inductive liner compression experiments have attained.6,11 For
concreteness, assumptions for the subscale tests were chosen to correspond to existing equipment at MSNW and the
Plasma Dynamics Laboratory (PDL) at the University of Washington. The dynamics of the liner implosion are
governed by the equation:

\[ M_L \frac{d^2 r}{dt^2} = \left( \frac{B_{m}^2}{2 \mu_0} - \frac{B_{e}^2}{2 \mu_0} \right) 2 \pi r w, \]  

(1)

where \( M_L \) is the liner mass, and \( w \) the liner width. During the rapid liner acceleration very little flux can diffuse
through the liner (i.e. \( B_{m} << B_{e} \)). Due to the inertia of a solid metal liner, it is possible to sustain the magnetic field
pressure (i.e. maintain a constant amplitude \( B_{e} \)) during this time by continually increasing the flux in the gap
between the coil and liner to counter the increasing gap cross-sectional area as the liner moves inward. This occurs
naturally for a simple L-C discharge circuit with an appropriately large capacitance. The near constant magnetic
field during this time is observed experimentally and was confirmed by 3D modeling with the Maxwell® 3D
electromagnetic code. With this approximation Eq. (1) is readily integrated to obtain the liner velocity \( v_L \). \( B_{e} \) is then
determined by the stored capacitor energy minus liner kinetic energy, \( E_L \). In a variant of the virial theorem, the
maximum transfer of the stored energy, \( E_s = \frac{1}{2} CV_c^2 \) into liner kinetic energy is found when half of this energy is
expended in the driving magnetic field energy, \( E_B \). By employing a circuit design with low stray inductance, \( E_B \) will
be concentrated primarily in the annular gap volume between the liners and the driving coils. One can thus derive an
expression for the compression magnetic field during the short distance \( \Delta r \) over which the main liner acceleration is
produced:

\[ E_B = \frac{B_{e}^2}{2 \mu_0} 2 \pi r_L \Delta r w = \frac{1}{4} CV_c^2 \Rightarrow B_e = 7.8 \times 10^{-4} \left( \frac{C}{w} \right)^{1/2} \frac{V_c}{r_L}, \]  

(2)

where \( B_e \) can be expressed as a function of only the initial liner physical dimensions and circuit parameters. Here \( r_L \)
is the liner initial radius. The radial distance over which the compression field remains large as the liner moves
inward, i.e. \( \Delta r \), was taken to be equal to \( r_L/6 \). This approximation was obtained from both experimental results and
analytical circuit calculations. Equating the remaining stored energy with the liner kinetic energy (Ohmic losses in
the liner and coil are calculated to be negligible here), one has then for the liner velocity:

\[ v_L = \left( \frac{C}{\pi r_L w \delta \rho_m} \right)^{1/2} \frac{V_c}{2}, \]  

(3)

where the liner mass, \( M_L = 2 \pi r_L \cdot w \cdot \delta \cdot \rho_m \) with \( \delta \) being the liner thickness, and \( \rho_m \) the density of the liner material.

The key process of the dynamical behavior of the convergent aluminum foil liners was analyzed by both a one
dimensional analytic model that contains all of the relevant electrical circuit equations to provide for the calculation
of the liner motion and heating due to changing magnetic fluxes and fields. The most accurate accounting of the
liner dynamic behavior was obtained with the ANSYS Explicit Dynamics® Solver (AEDS). Here the full three
dimensional non-linear behavior of the aluminum liners was modeled based on the magnetic pressure profile in time
and space similar to that predicted by Eq. (1) and ANSYS Maxwell®. The result of a calculation with a physical
setup similar in scale to the FDR prototype is shown in Fig. 4.
As mentioned, the FRC has been selected as the target plasma. There is practically no alternative plasma target to the FRC as it is the only closed field, magnetically confined plasma that has demonstrated the configuration lifetime scaling required for the relatively slow liner compression envisioned here. It is critical to have sufficient plasma confinement in order to retain plasma energy and inventory during the time required for the liner to reach peak compression. Even for the fastest implosion speeds achieved experimentally to date (~3 mm/µs), the time to maximum compression is several times the axial ion transit time. The FRC also has the distinct feature that even with a liner capable of only a 2D radial compression, the FRC will undergo an axial contraction due to the internal field line tension within the FRC, with the net result being effectively a 2.4D compression of the FRC. The energy within the FRC separatrix at peak compression is dominated by plasma energy that is in pressure balance with the edge magnetic field \( B_0 \). This allows one to write:

\[
E_L = \frac{1}{2} M_L v_L^2 = 3n_0 k T_0 \frac{4}{3} \pi r_0^3 e = \frac{B_0^2}{\mu_0} \pi r_0^3 e ,
\]

where the zero subscript indicates values at peak compression. The last expression in Eq. (4) reflects the reasonable assumption that \( r_s \sim r_0 \) and that the FRC plasma is in radial magnetic pressure balance \((2n_0kT_0= B_0^2 /2\mu_0)\). One has then for the fusion energy produced in the FRC during the shell’s dwell time \( \tau_D \) at peak compression:

\[
E_{\text{ fus}} \approx 1.2 \times 10^{-12} n_0^2 (\sigma v) \frac{4}{3} \pi r_0^3 e \tau_D = 1.1 \times 10^{-12} n_0^2 T_0^2 \frac{r_0^4}{\nu_L} \epsilon
\]

where \( n_0 \) and \( T_0 \) are the peak density and temperature. The liner shell dwell time at peak compression, \( \tau_D \), is approximated as \( \sim 2r_0/v_L \), the time it would take the liner to reach the axis unimpeded and rebound to \( r_0 \). The dwell time will actually be much longer for a thick liner as the outer liner surface continues to travel inward until the shock from the halting of the inner liner surface reaches the outer surface. This time can be much longer than the assumed \( \tau_D \) since \( r_{1,\text{outer}} \sim 6r_0 \). The more conservative dwell time is assumed here as liner compressive effects are also not considered in this zero order analysis. The usual approximation for the D-T fusion cross section in this temperature range \((5-40 \text{ keV})\): \( \langle \sigma v \rangle \approx 1.1 \times 10^{-13} T_0^2 (\text{eV}) \) was also assumed. Radial pressure balance, together with expressions (4) and (5) yields for the fusion gain:

\[
G = \frac{E_{\text{ fus}}}{E_L} = 1.73 \times 10^{-3} \sqrt{\frac{M_L}{l_0} B_0} = 4.3 \times 10^{-8} \sqrt{M_L \frac{E_L^{3/8}}{l_0^3}}
\]

where \( l_0 (= 2r_0 \epsilon) \) is the length of the FRC at peak compression. The last expression is obtained from the adiabatic scaling laws for the FRC (see Fig. 5):

\[
E_L \sim B_0^2 r_0^2 l_0 \sim B_0^{4/5} \quad \text{and} \quad l_0 \sim r_0^{2/5} \sim B_0^{-1/5}
\]

in order to express \( G \) in terms of the liner kinetic energy and mass, \( E_L \) and \( M_L \) only.

Starting with typical FRC parameters achieved in past experiments one obtains the final FRC parameters reflecting both radial and axial adiabatic compression from the 3D convergence of the liners. The ends of the merged liners are observed to do this naturally in the AEDS calculations (see Fig. 4), as a consequence of a significant, axially-inward liner motion. The unique response of the FRC equilibrium to axial liner compression is quite valuable in this context as it provides for magnetic insulation of the FRC boundary regardless of the increase in the ratio of plasma to magnetic energy that comes with the increased axial compression.

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While the FRC can be generated over a wide range of sizes, temperatures and densities and then translated into the liners for further compression, the proper plasma parameters for the initial FRC are best found by extrapolation back from the desired final state. The compression that is applied by the liners is adiabatic with regard to FRC as the liner speed is far less than the plasma sound speed. The key adiabatic relations for the FRC are stated in Fig. 5. The injection of the FRC is delayed until the liners have been fully accelerated and have moved inward away from the driver coils. For the validation experiments currently being constructed, two FRCs will be injected and merged inside the liner as this permits an axially stationary liner compression. This limits vacuum end wall damage and considerably eases the diagnostic evaluation of the compression process as the target remains fixed. Adding a translating component to the liner motion is straightforward and would be something to be addressed in the next phase of development of FDR.

The inward liner motion and compression ceases when the internal FRC energy has increased to the point where it stagnates the liner inward motion. At this point the plasma energy will roughly equal the initial liner kinetic energy. From Fig. 5 the final compressed FRC length is 35 mm at an internal pressure characteristic of a 410 T field ~ 67 GPa. Ideally, the capacitor energy storage and driver circuit at the UW is capable of generating liner energies with $E_L = 560 \text{ kJ}$. The 3D convergence of an Aluminum liner set with an initial total mass of 0.18 kg would produce a fusion gain $G = 1.6$. If realized, this would be an extraordinary achievement for such a modest experiment, and a testament to the cost and efficiency advantages of this approach to fusion.

The total gain desired from the FDR is determined by the energy requirements to vaporize, ionize and energize the metal liner propellant to achieve a suitably high Isp. It is useful then to rewrite Eq. (6) in terms of the fusion energy produced per unit liner mass, or

$$\frac{E_{fus}}{M_L} = G \left( \frac{E_L}{M_L} \right) = 4.3 \times 10^{-8} M_L^{15/8} v_L^{4.75}$$

(8)

where Eq. (4) was used to put the expression in terms of the explicit liner variables. It can be seen that increasing either the liner mass, or velocity will increase the energy input into each liner particle for higher Isp. There is however a velocity limit for a given liner material and thickness. This set by a material’s properties (electrical conductivity, melting point, and heat capacity) in order to avoid vaporization due to the inductive heating that the liner experiences during magnetic acceleration of the liner. As was first pointed out by Cnare in his landmark foil compression experiments, the liner’s minimum thickness (mass) for a given liner velocity can be characterized by a parameter $g_M$ defined by the “current integral”:

$$\int_0^{t_0} I^2 dt = g_M A^2$$

(9)

Figure 5. (Top) FRC adiabatic scaling laws, and (Bottom) Anticipated FRC parameters from merging, a purely radial, and a purely axial compression. During the actual liner implosion the FRC radial and axial compressions would occur simultaneously. They are calculated separately to show their relative effects.
where \( I \) is the current flowing through the material cross-sectional area, \( A = w \times \delta \), \( w \) is the hoop width and \( \delta \) the hoop thickness. The driving force is simply the magnetic pressure \( (B^2/2\mu_0) \) applied over the surface area of the shell facing the coil when in close proximity to the driving coil. The current can be related to the field through Ampere’s law which can be reasonably approximated as \( B = \mu_0 I/w \). Normalizing to the action constant for the vaporization of aluminum from an initial 300 °K, i.e. \( g_{Al} = 5.9 \times 10^{16} \text{ A}^2 \text{sec/m}^4 \), one finds for the maximum velocity for a given shell thickness \( \delta \):

\[
v_{\text{max}} = 6.8 \times 10^{10} \left( \frac{g_M}{g_{Al}} \right) \frac{\delta}{\rho_M},
\]

where \( \rho_M \) is the shell material density. While the liner thickness limits the launch velocity, once in motion further heating is no longer an issue, even during the final field compression, due to the thickening of the liner with convergence. To achieve sufficient gain, the liner initial thickness will typically be much greater than that needed for the characteristic velocities (2-4 km/s) anticipated.

There are potentially several metals that could be employed. Not surprisingly, aluminum is a strong contender due to its low density and high conductivity, but lithium is not far behind. For a given liner energy, its low mass density allows for thicker initial liner as well as a larger final shell radius. The latter is important for slowing down the fusion neutrons and extracting the maximum energy from the fusion products. Possessing a low yield strength, lithium also has several advantages as a plasma propellant. Recall that the ultimate fate of the shell is vaporization and ionization after intense fusion, ohmic and radiative heating. Lithium is to be favored for its low vaporization temperature and ionization energy thereby minimizing the frozen flow losses. Due to its low atomic mass it will also attain the highest \( I_0 \) for a given fusion energy yield. For these reasons, lithium is the propellant of choice for the FDR. From Eq. (10) one finds for lithium: \( v_{\text{max}} \text{ (km/s)} = 16 \delta \text{ (mm)} \). As will be seen, the anticipated lithium liner thickness is several mm so there is no real issue here as high gain can be accomplished with liner velocities of 3-4 km/s. For the validation experiment aluminum is the clear choice due to its wide availability, low cost, and ease in handling.

To achieve ignition, a fusion gain \( G > 5 \) is desired along with sufficient magnetic field for the magnetic confinement of the fusion product alpha (\(^4\text{He}\)) within the FRC plasmoid. With fusion alpha heating, ignition conditions are achieved and the effective gain can be significantly increased, potentially to as large as several hundred as noted above.

### III. Mission Analysis

Following the manned Moon missions, it was assumed that the next stepping stone towards mankind’s exploration of the solar system would be a mission to Mars. While mankind has certainly achieved many space milestones which have led to significant scientific discoveries, up to now manned space travel has been severely limited. The reasons for this can be boiled down to two main issues. Simply put, with current technologies manned exploration of the solar system: (1) takes too long and (2) costs too much. With a closer look at virtually all the issues encountered when considering a manned planetary mission, the main problem will come back to these two reasons. For example, space travel outside the protection of the Earth’s magnetosphere presents a myriad of safety issues for human beings. Foremost, there is exposure to radiation and high energy particles that can cause significant cancer risk as well as bone and muscle loss due to the lack of sufficient gravity. Both these health issues only become major issues for long durations in the space environment. Radiation exposure can be lessened by bringing massive shielding into space, and muscle and bone loss can be limited by creating artificial gravity. However to do so, would simply transfer these issues to the “cost too much” category. In addition to physical safety, there is also mental fatigue that can become problematic for long duration missions. Finally, and perhaps most catastrophically, long duration missions can have an increased risk of critical failure.

Beyond safety, there are also the issues associated with the political climate over long periods of time. Policies and program directives can change significantly from administration to administration, making large-scale, long term manned space exploration difficult to fund in a consistent way. Along those same lines, the general interest of the public must be maintained for long missions as well. While the aforementioned does not entail a complete list of the concerns associated with space travel it does provide good examples of the major issues that scale as a function of mission time.
Space operations have never been inexpensive endeavors, and the added complexity of manned spaceflight only adds to the cost. This is one of the major reasons for robotic exploration as is done currently. There are direct costs incurred with sending men into space, such as operational costs as well as the expenses associated with complex pre-deployed assets or on-orbit assembles usually required for manned planetary exploration. It is worth noting that both these direct costs also scale with mission length. Generally speaking, both operational and space asset cost go up significantly for longer duration missions. There are also launch costs required for any space mission. At $10,000 per kg to LEO, large space structures and fuel depots quickly come to dominate the cost.

A solution that addresses both of these two obstacles to manned space travel is a propulsion method that has high specific power, $\alpha$ (engine power/spacecraft mass) in addition to high exhaust velocities ($I_{sp}$). High specific power ($\alpha$ of order unity) to significantly reduce trip times, and high $I_{sp}$ (> 3,000 s) dramatically increase payload mass fraction, greatly reducing initial mass at LEO. The overarching design criteria therefore, is a mission architecture based on a propulsion system that can complete a manned Mars mission in 210 days using only a single launch from Earth. How this is to be accomplished with the Fusion Driven Rocket will now be outlined.

A. Previous Mars Mission Analysis

A manned Mars case study was chosen as this would clearly be the first destination for a planetary manned mission. Manned Mars missions have been analyzed many times over the ensuing decades after Apollo with a large variety of spacecraft and propulsion methods. The most recent and possibly the most detailed was that conducted by NASA in the 2000s. The results of that study were summarized in the Design Reference Architecture (DRA) 5 in 2009. Many of the aspects of this study, such as payload and habitat mass, were used as the starting point for the reference architecture for the FDR. In addition the NASA DRA 5 detailed the full scope of Mars exploration options, including launch, Earth orbital operations, trans-Mars injection (TMI), Earth-Mars cruise, Mars orbit insertion (MOI), Mars orbital operations, entry/descent/landing, surface operations, Mars ascent, on-orbit rendezvous, TMI, and Earth arrival. The DRA 5 also developed many figures of merit to evaluate what are referred to as Opposition-Class and Conjunction-class missions. Opposition-class missions are typified by short surface stay times at Mars (typically 30 to 90 days) and relatively short total round-trip mission times (500 to 650 days). The exploration community has adopted the terminology “short-stay” missions for this class. Conjunction-class missions are typified by long-duration surface stay times (500 days or more) and long total round-trip times (approximately 900 days). These missions represent the global minimum-energy solutions for a given launch opportunity.

What was concluded in DRA 5 is that the choice of the overall exploration mission sequence and corresponding trajectory strategy has perhaps the greatest single influence on the resulting architecture. It was stated that “the ideal mission would be one that provides: (1) the shortest overall mission to reduce the associated human health and reliability risks; (2) adequate time on the surface in which to maximize the return of mission objectives and science; and (3) low mission mass, which, in turn, reduces the overall cost and mission complexity.” It was also determined that the ideal mission did not exist, and it was clear it was principally due to the limitation in propulsive capabilities which resulted in stringent confinement to orbital mechanics and planet phasing. Basically, a short-stay mission approach would require departing Mars on a non-optimal return trajectory, while a long-stay approach time would be spent at Mars waiting for more optimal alignment for a lower-energy return. It is important to note that the risk assessment that was conducted in DRA 5 indicated that both the short-stay (Opposition-class) and the long-stay (Conjunction-class) mission option posed a high risk to crew members that would exceed the current permissible radiation exposure limits. It was concluded in DRA 5 that a Conjunction-class or long stay mission would be favorable. This was largely based on the criteria of Crew Health and Performance (CHP) components. This metric was broken down into Physiological Countermeasures, Human Factor and Habitability, Radiation, Behavioral Health and Performance, and Medical Capabilities. Even though the Conjunction-class mission showed an overall increase risk to Behavioral Health and Performance, as well as Medical Capabilities due to longer overall duration, it was favorable based on less 0-g transit phases and less exposure to free space heavy ion environment. The other major reason that was sighted as preferable for long-stay missions is the percentage of time spent at Mars compared to the total mission time. Again, due to lack of adequate propulsion, the Opposition-class loses out. However with increased propulsion capabilities it is not only possible to increase this percentage to a significant fraction even for short-stay times, it is also possible to lessen all the major CHPs including bringing the radiation exposure to with permissible exposure limits.

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B. Designing a New Mission to Mars

A top down approach was used to examine the effects of fusion propulsion on manned exploration of the solar system. This is the most sensible way to avoid having the fusion concept “tail” wag the mission “dog”. Given the large uncertainty in the maximum fusion gain, spacecraft $\alpha$ and Isp, it made more sense to specify the desired mission goals (see Table 1) first, and have that in turn determine the type and scale of the fusion system – assuming of course that the fusion system can provide the necessary $\alpha$ and Isp.

The first set of mission analysis performed for FDR was conducted using trade studies of fusion gain and single trip time from Earth to Mars. The objective of the work reported here was to expand upon a single case study to determine the exact fusion conditions that would be needed to achieve the ideal Mars mission as outlined in Table 1. To this end, two of the criteria were selected for this case study as most important: a 90 day transit to Mars, and a single launch of the spacecraft to LEO. The 90 day transfer was considered the most important parameter as it not only reduced the cost and safety risks of a manned mission to Mars, but was the simplest, if not only viable way to bring radiation exposure to within permissible limits. While missions faster than 90 days were certainly feasible with FDR propulsion, the $\Delta V$ budget increased significantly, driving down payload mass fraction, and ultimately increasing initial mass in low earth orbit (IMLEO). This leads to the second main criterion which limits the IMLEO mass to 130 MT or less. It was felt that this was an important element in the feasibility of manned Mars missions as it greatly simplifies the total mission plan and substantially reduces mission costs.

Beyond these two main mission criteria several other mission stipulations were set forth. Foremost was a set payload mass. For completeness and ease of comparison, the payload elements of the Crewed Mars Transfer Vehicle (MTV) were adopted from DRA 5. Depending on the mission type, Opposition-class or Conjunction-class, as well as the propulsion method selected, the masses of payload varied in the DRA 5 analysis. For this case study the largest payload of 62.8 MT was selected. The payload mass breakdown is shown in Table 2.

Two other mission stipulations for this study were the use of full propulsive orbit insertion maneuvers at both Mars and Earth return. Eliminating aerobraking at Mars reduces risk and complexity of the spacecraft and mission architecture. Furthermore it was shown in earlier analysis that the mass of the heat shield required for an Aerobraking maneuver is much more

<table>
<thead>
<tr>
<th>Mission Architecture Goals</th>
</tr>
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<tbody>
<tr>
<td>- 90 day transit times to and from Mars</td>
</tr>
<tr>
<td>- Single launch to Mars (130 MT IMLEO)</td>
</tr>
<tr>
<td>- No pre-deployed assets</td>
</tr>
<tr>
<td>- 63 MT Payload mass</td>
</tr>
<tr>
<td>- Full propulsive MOI</td>
</tr>
<tr>
<td>- Full propulsive EOI</td>
</tr>
<tr>
<td>- Reusable spacecraft</td>
</tr>
</tbody>
</table>

Table 1. Mission goals based of the objective of reducing transit times and mass required at LEO

<table>
<thead>
<tr>
<th>Payload Summary</th>
<th>Mass (MT)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Short saddle truss</td>
<td>4.7</td>
</tr>
<tr>
<td>Contingency food canisters</td>
<td>9.8</td>
</tr>
<tr>
<td>2nd docking module</td>
<td>1.8</td>
</tr>
<tr>
<td>Forward RCS prop load</td>
<td>3.2</td>
</tr>
<tr>
<td>Transit habitat</td>
<td>32.8</td>
</tr>
<tr>
<td>CEV/service module + crew</td>
<td>10.6</td>
</tr>
<tr>
<td>Total Payload Mass</td>
<td>62.9</td>
</tr>
</tbody>
</table>

Table 2. Payload summary from DRA 5. This table includes the Mars transit habitat as well as the supporting life support and subsystems

<table>
<thead>
<tr>
<th>Mission Assumptions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Payload mass</td>
</tr>
<tr>
<td>Spacecraft mass</td>
</tr>
<tr>
<td>Earth Orbital Altitude</td>
</tr>
<tr>
<td>Mars park orbit</td>
</tr>
<tr>
<td>250x33793 km</td>
</tr>
<tr>
<td>Capacitor specific mass</td>
</tr>
<tr>
<td>Solar panel specific mass</td>
</tr>
<tr>
<td>Tankage fraction</td>
</tr>
<tr>
<td>Isp</td>
</tr>
<tr>
<td>Fusion Gain</td>
</tr>
</tbody>
</table>

Table 3. Mission assumption based on the payload and park orbits from DRA 5. Specific masses and engine performance parameter assumed to fulfill the mission architecture goals stated in Table 2.
massive than the propellant needed by the FDR to perform the same ΔV maneuver. While chemical propulsion missions and even NTP propulsion show large mass saving by using aerobraking instead of more propellant, this is not true of a high Isp engine. Along similar lines there is the aero capture maneuver that is normally assumed upon Earth return. DRA 5 took into account that aerocapture at Earth was possible and well understood based on previous flight experience. It employed return trajectories with Earth entry speeds for a nominal Mars return trajectory that were as high as 12 km/s. This was deemed acceptable based on the 11 km/s required for the lunar Crew Exploration Vehicle (CEV). For this case study an Earth Orbit Insertion maneuver was conducted instead of relying on a direct entry approach from Mars. This was done for two reasons. First, it allows for the standard CEV to be used without necessitating the development of higher density, lightweight, thermal protection systems. Second, by allowing the spacecraft to enter into an earth orbit upon return from Mars, the FDR spacecraft would be ready for future missions simply by re-launching a new payload and additional propellant. As will be discussed later, the FDR spacecraft is designed as a reusable system.

### C. Mission Design Details

With the basic mission goals outlined, trajectory optimization was carried out using the COPERNICUS software. COPERNICUS is a NASA developed code that provides a single, unified framework for modeling, designing, and optimizing spacecraft trajectories for robotic and human missions. The methodology facilitates modeling and optimization for problems ranging from a single spacecraft orbiting a single celestial body, to a mission involving multiple spacecraft and multiple propulsion systems operating in gravitational fields of multiple celestial bodies. The model was set up to start with an initial (and final) Earth orbit of 407 km. This was done to allow comparison with the DRA 5 mission architecture. The parking orbit at Mars was also taken from DRA 5 as 1 sol orbit, which has a periapsis altitude of 250 km and an apoapsis altitude of 33,793 km. The mission was modeled using 7 segments: Trans Mars Injection (TMI), Trans-Mars coast, Mars Orbit Insertion (MOI), stay time, Trans-Earth Injection (TEI), and an Earth Orbit Insertion (EOI). Segment functions were setup to limit the entire mission time to 210 days and mandates that the Mars stay time be no less than 30 days. The mission architecture was also set up so that the payload mass of 63 MT was dropped off at Mars and the 15 MT spacecraft mass was returned to earth. The spacecraft mass assumed here is based on first iteration design efforts and spacecraft scaling optimization that was conducted in previous work. A list of the mission parameters can be found in Table 3. The COPERNICUS code was employed to find a minimum ΔV trajectory for these mission parameters. The code was allowed to optimize departure date as well as the length of all 4 maneuvers (TMI, MOI, TEI, EOI) as well as the coast times. COPERNICUS optimized to a slightly shortened trip time to Mars of 82.9 days and a return trip time of 97.1 days. The total ΔV budget for the mission optimized to a minimum of roughly 50 km/s. The ΔV as well as the burn time of each maneuver is listed in Table 4.

The original trajectory optimization was conducted using a simplified orbital model in order for COPERNICUS to perform a wider range of parameter sweeps. This model allowed for finite burns and coast times. The COPERNICUS visualization of the ΔV optimized trajectory for a 210 day manned Mars mission consists of a 82.9 day Earth-Mars transit, a 30 day stay, and a 97.1 day Mars-Earth return.

<table>
<thead>
<tr>
<th>Maneuver</th>
<th>ΔV (km/s)</th>
<th>ΔT (days)</th>
<th>Mi (MT)</th>
<th>Mf (MT)</th>
<th>Mp (MT)</th>
</tr>
</thead>
<tbody>
<tr>
<td>TMI</td>
<td>7.3</td>
<td>7.1</td>
<td>133.4</td>
<td>115</td>
<td>18.4</td>
</tr>
<tr>
<td>MOI</td>
<td>13.2</td>
<td>10.5</td>
<td>115</td>
<td>87.8</td>
<td>27.2</td>
</tr>
<tr>
<td>TEI</td>
<td>16.5</td>
<td>2.9</td>
<td>26.8</td>
<td>19.2</td>
<td>7.6</td>
</tr>
<tr>
<td>EOI</td>
<td>12</td>
<td>1.6</td>
<td>19.2</td>
<td>15</td>
<td>4.2</td>
</tr>
</tbody>
</table>

Table 4. Mission Maneuvers

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periods, but did not fully model the escape and capture maneuver’s required at both Earth and Mars. Therefore it was necessary to examine in detail the near body orbital mechanics and the required maneuvers to enter or exit their gravitational influence. Figure 6 depicts the results from COPERNICUS with finite burn maneuvers for TMI, MOI, TEI, and TOI. All of the ∆Vs for these maneuvers were within 2% of the ∆V determined from the simplified full mission profile optimization except for the TOI maneuver. This maneuver, as shown in Fig. 6, required an additional impulsive maneuver in order to circularize the orbit at the 407 km LEO orbit. This was done to allow COPERNICUS to converge to a solution using rather high thrust impulse burns. A more optimized Earth Orbit insertion maneuver will be calculated in future mission designs, but for this preliminary design the ∆V budget presented in Table 4 is sufficient.

With the ∆V determined for an ideal Mars mission that satisfies both criteria (1) and (2) as stated in DRA5, the final criteria (3) is to be determined by the characteristic specific impulse of the propulsion system. This final criteria is a low mission mass, and it was the goal of this case study to have the mass small enough to enable a single launch to Mars. Based on projections for future heavy lift vehicles, the mass limit for IMLEO is 130 MT. It is also worth noting that if future heavy launch vehicles cannot achieve this metric the mission architecture for this case study would simply require two separate launches and a single on-orbit rendezvous. In this scenario it would be speculated that the FDR spacecraft would be sent up first and a pre-mission check would be conducted including main FDR testing without the crew members on board. The second launch would be the payload plus crew. This type of system checkout is likely to be desirable in either case.

Within the COPERNICUS code, propulsive maneuvers can be determined using any number of thruster parameters. For this study an Isp of 5000 s was chosen to keep the initial spacecraft mass less than 130 MT. This Isp value is consistent with a fusion gain of 200. With an Isp of 5000 s and the optimal ∆V budgets for the specified mission requirement, as well as the specified payload and spacecraft mass, COPPERNICUS calculations determined that a jet power of 36 MW would be needed to complete the mission. With the power defined, an overall picture and scaling of the spacecraft itself is now possible.

As was stated, the objective was to dramatically improve upon current mission Mars architectures in order to bring a manned mission within fiscal and conceptual reach. Design architectures that use conventional chemical propulsion require up to 12 heavy lift launches and as much as 1,252 MT in LEO. With Nuclear Thermal Propulsion this mass can be reduced to 849 MT over 9 launches. This is compared to a single launch of 134 MT for Fusion Driven Rocket architecture. These metrics of comparison are summarized in Table 5. The DRA architectures require significant pre-deployed assets at Mars prior to a manned mission. This includes propellant for the return trip home as well habitats and supplies for a stay time of 539 days. And while this case study assumed the 63 MT payload of the manned portion of the DRA architecture it did not presume to include any of the pre-deployed assets as the stay time was reduced to 30 days and all the propellant need for the round trip mission would

<table>
<thead>
<tr>
<th>Mission Comparison</th>
<th>FDR</th>
<th>DRA 5 NTP</th>
<th>DRA 5 chemical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of launches</td>
<td>1</td>
<td>9</td>
<td>12</td>
</tr>
<tr>
<td>IMLEO (MT)</td>
<td>134</td>
<td>849</td>
<td>1252</td>
</tr>
<tr>
<td>Mission time (days)</td>
<td>210</td>
<td>914(1680)</td>
<td>914(1680)</td>
</tr>
</tbody>
</table>

Table 5. Mission launch requirements. Mass required in LEO, and the overall mission time for the 210 day FDR Mars mission compared to the DRA architecture using both Nuclear Thermal Propulsion (NTP) and chemical propulsion systems.
be carried in the original spacecraft. Because the architecture requires pre-deployed assets to be placed at Mars before the mission can begin, the total mission time from start to finish is 1680 days.

IV. Spacecraft Design

Based on the mission down design approach, requirements have been set forth for a spacecraft that is less than 15 MT and is comprised of a rocket engine that can produce 36 MW of jet power at an Isp of 5000 s. This section will focus on the limitation of 15 MT for the spacecraft dry mass, and detail how the FDR design can satisfy this design requirement.

One of the most significant masses in the FDR concept is the energy storage system required to energize the liners. This is accomplished with high voltage, pulse capacitors. Using the straight gain equations from the fusion physics section D, and assuming an additional enhancement from ignition of 10 to achieve a fusion gain of 200, a total liner kinetic energy of at least 2.8 MJ will be required. A total liner mass of 0.5 kg results in an Isp ~ 5000 s as desired. To achieve an average jet power of 36 MW with 90% conversion efficiency will require a rep rate of 1/14 sec providing sufficient time for liner reload and recharging the energy storage systems. It will be assumed that the stored (bank) energy must be at least twice the liner kinetic energy. A coupling efficiency of 45% is assumed which, as was mentioned earlier, is near the optimum coupling efficiency and is consistent with the 1D circuit modeling. A 6.2 MJ bank of capacitors is thus required. Commercial high voltage, high energy density, pulse capacitors have demonstrated energy densities as high as 3 J/g. While improvement in performance can be expected in the future, the assumption here for the FDR spacecraft design will be 2.5 J/g reflecting a devaluation for space rating and margin, and resulting in a total capacitor mass ~ 2.5 MT. Based on laboratory experience, the energy delivery system (SEP converters, charging system, start and crowbar switches, housings, support structures, power feeds, cable, and stripline) will scale with the capacitor mass. A very conservative value of roughly half however is assumed or 1.2 MT.

The second major power system component that is required are solar panels. It is important to note that the Fusion Driven Rocket, at least as it is envisioned for its first flight mission, will power the fusion reaction using electrical energy derived from solar panels. There are several reasons for this. First, solar panels have a long flight heritage and a proven performance record in space. They have flown on over 99% of space missions launched to date. Second, while energy could certainly be obtained from the flux compression occurring during propellant expansion out of the rocket engine, this adds complexity and risk. While this type of energy recovery may be incorporated later in a fusion rocket development program, it was not felt to be critical to the concept feasibility.

The current state of the art solar panels (e.g. the MegaFlex program) are expected to generate over 200 W/kg, and this value was used in calculating the solar panel specific mass. It should be noted that the development of much higher density solar arrays are anticipated in the near future. It has been predicted that 500 W/kg, possibly up to 1000 W/kg would be possible with advanced III-V multi-junction cells. At a fusion gain of 200 the 36 MW of jet power needed for the 210 day Mars mission will thus require 180 kW of solar power. This is the solar power that will be needed throughout the mission; including Mars were the solar irradiance is 56% less. Since panel performance metrics such as specific mass are scaled for Earth irradiance, the solar panel system mass for FDR was scaled up by a factor of 2.25 to 2 MT for the aforementioned solar panels with an Earth α of 200 W/kg.

As was described earlier, the Fusion Driven Rocket is comprised of main liner compression coils as well as coils to create a divergent magnetic field at the exit. The mass of these coils is estimated based on them being high variations. The 33st International Electric Propulsion Conference, The George Washington University, USA

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Table 6: FDR Spacecraft Mass Budget

<table>
<thead>
<tr>
<th>Spacecraft Component</th>
<th>Mass (MT)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spacecraft structure</td>
<td>3.4</td>
</tr>
<tr>
<td>Lithium containment vessel</td>
<td>0.1</td>
</tr>
<tr>
<td>FRC formation system</td>
<td>0.5</td>
</tr>
<tr>
<td>Propellant Feed mechanism</td>
<td>1.2</td>
</tr>
<tr>
<td>Energy storage</td>
<td>2.5</td>
</tr>
<tr>
<td>Liner driver coils</td>
<td>0.3</td>
</tr>
<tr>
<td>Energy delivery system</td>
<td>1.2</td>
</tr>
<tr>
<td>Solar Panels</td>
<td>2.0</td>
</tr>
<tr>
<td>Thermal management</td>
<td>1.1</td>
</tr>
<tr>
<td>Magnetic expander</td>
<td>0.2</td>
</tr>
<tr>
<td>Margin</td>
<td>2.5</td>
</tr>
</tbody>
</table>

Spacecraft Mass $15$  
Crew habitat (DRA5.0) $63$  
Lithium Propellant $56$  
Total Mass $134$
strength aluminum with the appropriate cross sections to be structurally sound, and capable of handling the required currents and impulsive loads. This resulted in a total mass of 0.5 MT. These coils will certainly be fabricated taking advantage of modern, lightweight, high field structural materials such as SiC-SiC composites and other materials suitable for a neutron and space environment. The conservative estimate however provides for margin. Certainly carbon composite structures would also be used to provide rigidity to the coil assemblies.

A thermal management system will also be needed. This system will most likely consist of a working fluid that will be pumped through the high heat flux components such as magnetic coils and power electronics. The fluid will be radiated through space radiator panels. Detailed MCMP calculations of the neutron, gamma and particle physics are underway. With a more detailed understanding of the energy deposition in the various structures, a more in-depth design of the thermal managements system can be made. For now it is assumed that a large fraction of the neutron energy will be absorbed and used in heating of the liner as discussed in Section II. Given the large stand-off, along with the dimensional thickness of most of the structures, the energy deposition from the fusion neutrons will be small. It will be assumed however that 10% of the fusion energy is absorbed and 360 kW of heat rejection is required from the radiators. For high temperatures, space radiator specific mass of 1 kW/kg is quite conceivable. For this case study, due to the uncertain nature of the heat load to the engine subcomponents, a design margin of a factor of three was added. As a result 1.1 MT was allotted for the thermal control/heat rejection system.

In addition to the liner compression mechanism, the Fusion Driven Rocket requires a fusion plasma. The mass of the apparatus required for the generation, translation and injection of the FRC plasmoid must be included. The mass of this system is based on that employed in laboratory devices. Such a system will not be that dissimilar to the one to be used in the validation experiments to be discussed later, and would weigh no more than 500 kg. At first glance this appears to remarkably small, but it should be recalled that the vast increase in plasma energy required for fusion is being supplied by the liner energy (see Fig. 5), and that the initial FRC energy is only 2.2 kJ.

It should also be noted that even though the fusion fuel (50% deuterium/tritium mix) requires gaseous tank storage, the fuel mass required is insignificant. From the COPERNICUS calculations, the total energy required for the complete trip to Mars and return to Earth requires a total of 69 Terajoules. Each fusion event consumes one triton and one deuteron, and produces $2.82 \times 10^{12}$ J so that $2.43 \times 10^{25}$ tritons and deuterons are required. This amounts however to only 120 g of tritium and 80 g of deuterium fuel for the entire trip.

The final two major spacecraft components relate to the propellant mass. The primary propellant for the Fusion Driven Rocket will likely be composed of the lithium in the form of liners. Since lithium is a solid at room temperature, a low mass propellant storage system can be employed with a minimal tank mass fraction. For the purpose of this study it was assumed a constant tankage mass of 100 kg. The propellant feed mechanism on the other hand will require more mass. This device is responsible for assembling and injecting the liners into the magnetic coils before each thruster firing. The optimum method is clearly one that requires the least amount of complexity on orbit, therefore it is assumed that the liner material will be completely fabricated to the required specification on Earth and then loaded on to a roll. These rolls would then be used to form the liner hoops that would be guided mechanically, and injected electromagnetically at low velocity into position under the driver coils prior to driver coil activation. This method would also allow for layering of material within the liner to optimize for lower Ohmic losses, better neutron energy absorption and liner stability. While the envisioned process appears straightforward, a large mass budget of 1.2 MT is specified due to the lack of a detailed assembly design at this point in the design.
The spacecraft structural components include all of the remaining subsystems normally included in a spacecraft design. This includes fairings, support structures, communication systems, data handling ACS, and battery power system. An important aspect of the support structure is a shock absorbing system that interfaces the FDR with the spacecraft structure. The total mass for the spacecraft structure is therefore given the largest mass budget of any subcomponent in this analysis at 3.4 MT. In an attempt to be conservative, an additional margin of 20% for the entire spacecraft mass budget was included in addition to the margin and de-rating factor discussed for individual components. As reflected in Table 6, all of these components result in a spacecraft dry mass of 15 MT. With the 63 MT payload and the 57 MT of lithium propellant, the total IMLEO mass is 134 MT. It was clear in performing the analysis that there may be several areas where there are potentially large mass savings. Possibly the largest being the payload taken from DRA 5 which had a much longer Martian stay. The Apollo command and service modules together weighed only 30 MT. Given newer materials and greater knowledge of the space environment, a much smaller payload mass for the 30 day Martian sortie mission is envisioned as the design is refined. With the smaller payload, the performance metrics of gain and efficiency for the FDR can be less demanding, while still maintaining the total spacecraft mass at 130 MT or less for the 210 day mission.

Details of the Fusion Driven Rocket are shown in Fig. 8. This schematic shows all the major components of the engine at their relative scale. The engine is approximately 3.4 m in length from shadow shield to the end of the engine truss. The engine truss acts to support the 3 main compression coils as well as the magnetic expander. An open truss design was used to create the largest possible open area as well as to reduce weight. This open area allows for un-captured neutrons to escape the engine without causing additional heating or activation. The truss is 2.25 meter in diameter and is attached to the shock absorber plate. This plate transfers the shock from the pulsed fusion reaction to the rest of the spacecraft. This helps reduce or eliminate structural vibration especially on sensitive subcomponents such as the solar and radiator panels.

The lithium-based propellant is stored on 1.6 meter diameter spools, 9 m in length. Each spool would weigh approximately 9.7 MT. Six spools are arranged azimuthally around a seventh central spool for a total propellant mass of 68 MT of propellant. A good packing fraction is produced by this arrangement, and it also provides for all of the material to fit within a 5 m diameter saddle truss. This packing arrangement also affords additional radiation shielding, although adequate shielding is obtained by thick, permanent, graphite composite shields placed adjacent to the FDR. This shield placement also acts as a shadow shield for all of the spacecraft components including solar panels. A saddle truss was employed to facilitate refueling and reuse of the FDR spacecraft. It also provides for the option of a propellant or equipment drop for an even faster 90 day round trip Martian mission (30 day transit with a 30 day stay). This mission would likely require fuel pre-deployment at Mars.

The heat rejection radiator system is also attached to the saddle truss. They are approximately 5.2 m wide and 7.7 m long with a surface area 120 m². The radiators have been profiled to stay within the shadow shield to limit neutron exposure. Located at the forward most end of the saddle truss is the energy storage and electronic components to power the main compression coils as well as the magnetic field coils. This compartment also contains all of the power conversion modules and capacitor charging supplies. The power is fed down along a box frame truss on the side of the saddle truss to the FDR in an insulated and cooled stripline configuration. In this configuration, the
saddle truss and the attached components can be classified as part of the propulsion system of the spacecraft. It includes the engine itself as well as all the power systems, cooling systems, and propellant. The propulsion system is attached to the rest of the spacecraft via a 9 m long spine truss. This truss allows more stand off from the propulsion system, reducing the size required of the shadow shield. The spine truss also acts as a good separation point to modularize the spacecraft if required and would provide a location for additional equipment and payload to be stowed or attached. At the forward most end of the spine truss is the main solar panels and the communication subsystem. The solar array is located here to place it well inside the shadow. Each solar panel is 4.2 m wide and 15 m long adding up to a total surface area of 126 square meters. The Mars Transhab is 8.2 m in diameter and 11 m long and would mostly likely be composed of an inflatable structure. At the very front of the vehicle is the Mars Lander. The spacecraft length is 34 m in total. The component design was carried out mindful of the diameter limits of future planned payload fairings. This of course requires the use of deployable solar and radiator arrays, inflatable habitat, and possibly a compressible spine truss section.

V. FDR Experimental Validation

The greatest challenge for the FDR concept is in demonstrating the feasibility of inductively-driven, metal liner compression of the FRC plasma to fusion ignition. An experiment is now underway at MSNW and the Plasma Dynamics Laboratory (PDL) at the University of Washington to address this challenge. The initial results are presented here

A. Previous work

Inductively driven liners have been used for years to obtain the largest non-explosively driven magnetic fields of up to 610 T.6 A field of this strength would be considerably more than that required for compression of the FRC to achieve substantial fusion gain. The feasibility of rapidly accelerating inward and compressing thin hoops of aluminum and copper inductively was first demonstrated by Cnare [10]. Since then, the technique has been employed in several experiments to obtain very high magnetic fields in a small volume, which is certainly a result that is highly desired here as well. There are many advantages inherent in this approach, large stand-off from debris, electrical and physical isolation from the target, and magnetic insulation of the driver system from high energy particles to mention a few of the most crucial ones. Another great advantage is simplicity. Even though there is essentially no magnetic field within the liners initially, there is enough leakage flux during the inward acceleration that at peak compression the magnetic field that is trapped inside the now thickened metal wall thermally isolates and magnetizes the target plasmoid.

After the groundbreaking experiments performed by Cnare in the early 1960s, an inductively driven liner similar to those to be employed in the current experiments at PDL, was realized in experiments by Turchi et al.19 at NRL (see Fig. 10) in the early 70s. Large compression ratio convergence (~ 30:1) was obtained employing a thin (1 mm), large diameter (30 cm), but axially short (7 cm) aluminum liner. Peak magnetic fields as large as 140 T were achieved with excellent symmetry and quality employing only a 540 kJ capacitor bank.

As was noted earlier, the Cnare experiments as well as later experiments, there is a rapidly diminishing liner acceleration after the liner has moved inward roughly 20% of the coil radius. This is due to the drop-off in magnetic force as the liner moves away from the coil which limits the effective radial distance over which it is possible to efficiently maintain significant magnetic pressure. The “stroke length” can be significantly increased by increasing the radius of the driver coil/liner. By increasing the initial liner radius the distance over which one has to accelerate

Figure 10. Sequence of images of a backlight aluminum liner implosion (from Ref. 19).
the liners to a given velocity increases. This in turn allows for a significantly lower axial magnetic field to be employed to achieve the same final liner velocity. With the liner’s increased circumferential length, the total mass accelerated by the same axial field coil is significantly increased as is the liner kinetic energy.

Driving a liner with as large a radius as envisioned here for the FDR prototype \( r_c = r_L = 0.4 \) m has never been demonstrated, let alone an array of liners. This demonstration therefore became the first order of business in the FDR concept validation

B. Inductively Driven Liners at Large Radius

The initial liner tests were conducted at the scale desired for the prototype FDR with the coil radius of 0.41 m. The facility at the UW is equipped with a high voltage (up to \( \pm 25 \) kV) capacitor bank with a stored energy as large as 1.0 MJ. For the initial liner implosion experiments only a fraction of this bank was employed (870 \( \mu \)F at \( \pm 15 \) kV for a total stored energy of 392 kJ) to avoid significant collateral damage in the early testing. The AEDS analysis for the prototype FDR with three converging liners (see Fig. 2) was based on the following. It was assumed that each liner was driven by a capacitor bank with an initial energy storage of 335 kJ. The testing of one liner can thus be performed at similar energy to the AEDS calculations for comparison. The first tests were conducted with 0.4 m radius aluminum liners that were 6 cm wide, and 0.4 mm thick with a resultant mass of 0.16 kg. A schematic of the FDR test bed is shown in Fig. 11. The initial driver coils were energized by an array of 48 capacitor modules each consisting of five 25 kV 14.6 \( \mu \)F capacitors. A pair of D size ignitrons in series was employed for the start as well as crowbar switches. They were all triggered simultaneously by a single 25 kV pseudospark switch assuring simultaneity. The modules were divided in pairs connected in series to increase the maximum voltage (nominally \( \pm 25 \) kV). The 24 module pairs were then connected in parallel to the feedplate of the driver coil via 384 high voltage coaxial cables to minimize the stray inductance (0.07 \( \mu \)H), which was roughly 5% that of the vacuum coil inductance (1.4 \( \mu \)H). The energy coupling efficiency is strongly dependent on having the liner as close as possible to the coil at startup. The liner however acts to shunt most of the coil inductance before the liner moves inward. Making the stray as small as possible is critical to maintaining the magnetic energy in the gap during liner acceleration. In fact it is important that the stray inductance still be small compared to the inductance of the shunted coil. To a good

![Fig. 11. Fusion Driven Rocket liner compression test bed for liner validation experiments.](image)

**Figure 12.** Experimental End-on images (left) and AEDS code results (right) for a 0.4 m radius, 0.16 kg aluminum liner. The stored energy was 175 kJ (\( \pm 10 \) kV, 870 \( \mu \)F). The time refers to discharge initiation. Aperture in experimental images is at 14 cm radius. Internal probe wires can also be seen on axis.
approximation the initial coil-liner system appears as a stripline whose inductance is determined by the liner width $w$ (6 cm), coil-liner gap distance $\delta_{\text{gap}}$ (1.3 cm), and liner circumference, i.e. $L_{\text{gap}}$ ($\mu$H) $\sim (2\pi r_c)\delta_{\text{gap}}/w \sim 0.56 \mu$H.

The prototype-scale liner convergence tests were performed with aluminum liners in the G-10 vacuum chamber with a driver coil pair as illustrated in Fig. 11. The liners were fabricated from aluminum 1100 strip that was seam welded together and annealed. The weld was ground to maintain as best as possible the thickness, thermal and resistive properties of the bulk material. The liners were placed inside the vacuum chamber as indicated in Fig. 11. While the vacuum wall increases the gap considerably from what would be employed in a space based driver, it was necessary here to avoid issues with atmospheric interference, and would have been required in any case for the FRC plasmoid formation, translation and liner compression experiments.

The principle diagnostics that were employed to determine liner position as a function of time were several internal magnetic probes on axis, as well as external axial flux and B loops. End-on images of the liner motion were also obtained with a backlit fast framing camera as in the Cnare and Turchi experiments. These images yield detailed information regarding liner uniformity during convergence. In order to avoid confusion, a single liner was installed and only one coil energized. The resultant images from the experiment as well as similar constructed “images” obtained from the 3D AEDS calculation are shown in Fig. 12. It should be noted that these images were obtained for only the final 14 cm of the liner’s radially inward travel as the vacuum chamber end cones (see Fig. 11) blocked visual access at larger radius. The AEDS calculations were carried out with the same material, dimensions and magnetic pressure time history as the liners. The near identical results validate the use of the AEDS code for accurately predicting liner dynamics in designing future liner implosion systems. The buckling seen in both experiment and calculations occurs fairly early in the implosion. It appears that the early buckling serves two useful functions in that it minimizes the energy lost to compressional internal energy in the liners, and, as the liners move inward, the buckles naturally merge together to form a thick, compact stable wall at peak compression as desired. The predicted liner velocity and the actual liner velocity were quite close as can be seen in Fig. 12.

It should be noted that not all of the liner was observed to converge uniformly in the experiment as Fig 12 shows quite clearly. The liner section near the feedplate is retarded as it did not achieve the same inward velocity as the rest of the liner. This was found to be due to the thick aluminum feed plates causing the return magnetic field outside the coil to divert azimuthally around them near the feedplate gap. This significantly lowered the field in the gap at that location. Remarkably, this “tardy” section the liner did not appear to cause any major issues until it was sectioned off late in the implosion. The feedplate does not need to be a thick conductor as all the coil current flows in the first

![Figure 13. Circuit and liner parameters from 1D model for FRC compression experiments. Results are for two 10 cm radius, 5 cm wide, and 0.5 mm thick liners driven by 390 kJ bank at ± 15 kV with 70 nH stray inductance.](image-url)
few skin depths (~1 mm) of the inner wall. A redesigned thin (7 mm) feedplate backed with G-10 (5 cm) reinforcement produced liner implosions that exhibited no such asymmetry.

Interestingly, virtually all of the damage generated by the imploded liners was created by axial jets consisting of aluminum vapor and, for lower kinetic energy liners, small bits of Aluminum fragments. There was little if any damage to the vacuum wall under the driver coils. The conversion of radial kinetic energy into axial kinetic energy appears to be a natural consequence of magnetized liner implosions. The high energy liners were rapidly heated and melted by Ohmic currents flowing in the liner. As the liner collapses on axis, the magnetic field increases dramatically (see Fig. 13) as the axial magnetic field, which had diffused through the liner during the initial acceleration, is rapidly compressed to very high values. The metal liner acts to exclude this field and the rapidly increasing induced current quickly heats, melts and vaporizes the liner as anticipated. However without heating from the fusion event, there is no significant liner ionization. The axial jet-like behavior of the aluminum vapor is thus not a result of a plasma interaction with the axial magnetic field, but a consequence of the magnetic field on the implosion physics while the liner is still intact and a good conductor. Since magnetic field effects are not yet a direct part of the AEDS calculations, this process is best studied and understood using the 1D liner code that includes the behavior of all the relevant fields, fluxes, Ohmic heating, and circuit behavior. The results for the liners to be employed in the FRC compression experiments are shown in Fig. 13.

C. Inductively driven liners for FRC compression experiments

For the FRC formation, translation, and compression experiments it was decided to employ smaller coils of similar width (5 cm), but much smaller radius (10.3 cm). The primary reason is related to the speed of the liner implosion using the same energy storage, but divided over multiple liners. The aluminum liner thickness was required to be 0.4 mm to avoid both significant Ohmic heating during acceleration, and flux bleed through that would be well in excess of that desired for later FRC injection. While the kinetic energy of these more massive liners could be made sufficient for a fusion gain experiment, the liner velocity given the available bank was roughly 1 mm/μsec. The time required for the liner to converge, assuming an FRC injection at rL ~ 10 cm would be at least 100 μsec. While it is possible to generate an FRC with the requisite lifetime at this scale, it was not possible with the
financial resources of the project to fabricate the appropriate plasma sources, coils and pulse power supplies. The smaller coil, with its associated vacuum components, energy storage, and delivery systems solved this problem, and also allowed for much easier modification and replacement when needed.

The initial tests at smaller radius were conducted employing two straight wall cylindrical coils as in the larger radius setup. The same capacitor bank was used resulting in a driver magnetic field that was significantly increased which acted on a liner whose mass was significantly decreased, thus providing for a potentially much higher liner velocity. There was however some scaling trends that made this less than optimum. While the stray inductance was unchanged, the new coil had a much lower inductance, both in vacuum (0.19 μH) and with liners (63 nH) which was now comparable to the stray inductance which remained essentially the same. The effective coupling was thus significantly reduced. A schematic of the device is found in Fig. 14. Two liners were now employed as this will be necessary for 3D compression of the FRC. Both the 1D code and the AEDS were modified to reflect the new liner system. The results from the 1D code are found in Fig. 13 and the results from the 3D AEDS calculations can be found in Fig. 15. The gross dynamical behavior is quite similar for both codes and compare well with the experimental results. The experimental end-on images also appear very similar to the AEDS calculation although the internal axial probe obscures the liner behavior at touch down on axis.

There is some axial non-uniformity detected in the 3D calculations. This is primarily due to the stronger magnetic field found initially at the edges of the driver coils. The increased radial pressure causes the liner edges to arrive on axis a bit earlier. Experimentally this behavior also caused the internal magnetic probe to be terminated prior to peak field at the center of the liners where the 10 turn, 7 mm diameter pickup coils were located. A comparison of the internal magnetic field observed to that predicted by the 1D code is shown in Fig. 16. The rapid increase of the trapped magnetic field inside the liner is clearly observed for both however the rate of increase is somewhat less than that found in the code. A plausible reason is for this is that the internal cross-sectional area inside the liner is no doubt proportionately larger at small radius due to the azimuthal modulation of the inner wall from the previous buckling. This is clearly observed in the AEDS calculations but would not be reflected in the 1D code. Even with

Figure 16. Comparison of the experimentally measured internal B and that predicted by the 1D code. Code results were shifted in time to compensate for experimental timing delay as well as a somewhat slower axial implosion.

Figure 17. AEDS® calculation for the liner implosion for the smaller driver coil. Initial conditions were set to match anticipated experimental parameters. Color scale is in units of m/s.
this difference, internal axial magnetic fields well in excess of 100 T are inferred by the measurements as well as both of the codes.

D. Experimental Design for the inductively driven liner compression of an FRC plasmoid

In the next set of experiments the prospect of converging liners will be studied in preparation for the 3D FRC compression experiments. In order to create both an axial and radial acceleration of the liners, the driver coil is machined to have a conical pitch to the inner wall. With a matching conical liner the flux conserving nature of both surfaces assures that the accelerating magnetic field is parallel to both thus producing a magnetic pressure component normal to the surface that has both a radial and axial component. As a function of z, the strength of the magnetic field decreases as 1/r toward the large end of the coil and liner. Both the axial and radial components of the force, F acting on the liner scale as $P_B/A \sim B(z)^2/2 \mu_0 \cdot 2\pi r_l(z)w$ which therefore scales as 1/r. Since the liner mass per unit length increases linearly with r, the liner acceleration per unit length will scale as $F/mL \propto 1/r^2$.

The cone angle of the liner and coil thus need not be very steep to generate a significant axial acceleration of the liner as well as an increasing pitch to the liner as it moves in radially. This heuristic argument was born out by the AEDS calculations. The ideal convergence would result in the FRC trapped inside the liners with the touchdown of the liners first occurring on the outside ends. The staged arrival of the liner on axis creates a rapid pinching motion axially inward. In this manner a 3D compression of the FRC is produced at peak compression similar in behavior to that of a shaped charge.

The results from the AEDS calculations for the conical liners are found in Fig. 17 for the experimental setup shown in Fig. 14 which employs the same stored energy and delivery as

![Figure 18. Schematic of FDR validation experiment atop with magnetic flux contours 2D magnetic vacuum solver below. Liner and coil inner boundaries shown as red lines in calculation.](image)

![Figure 19. Flux lines and pressure contours from 2D MHD calculation for FRC formation and insertion into converging liners. Times refer to the start time for coil driver initiation (see Fig. 18). Contours from red (high) to blue (low) are normalized to maximum and minimum plasma pressure at each time.](image)
the straight coils experiments. The cone angle in the driver coils is 10 degrees with the small end the same radius as the straight coils (10.3 cm). The initial axial separation of the liners and driver coils is increased from 2 cm to 7 cm to accommodate the axial motion. As can be seen in Fig. 17, the liners move in axially, closing this gap to essentially zero at termination. The plan is to form and inject the FRCs after the liners have moved into the position found at \( t = 40 \mu\text{sec} \) in Figs. 17 and 18. The magnetic environment inside the vacuum chamber at that time is solved for using a 2D magnetic field vacuum solver that correctly treats both coil and liner as flux conservers. A plot of the magnetic flux inside the chamber at three characteristic times during the liner implosion prior to FRC formation and injection is found in Fig. 18. It can be seen that the liners prevent any significant flux inside the liner, but that external flux contours extend well beyond the liners once the liner moves in radially. This behavior is actually advantageous as it keeps the FRCs from expanding radially as they exit the conical formation coils and merge, and it tends to keep the resultant FRC located inside the liner until the fields within the liner increase significantly at small radius. The presence of the large magnetic field radially outside the liners also serves to maintain the FRC radially inside the liners even though there is initially a fairly wide gap at insertion (see Fig. 19).

Detailed 2D, resistive Magneto-Hydrodynamic (MHD) calculations have been carried out to study and optimize the FRC formation and merging in the appropriate geometry for insertion into the two converging liner bands. It appears that for the \( \textit{in situ} \) case (no overall translation of the liners), that two liners should be sufficient and even optimal to assure proper axial and radial compression of the FRC. The results from a 2D MHD calculation of FRC merging with two liners for the actual coil and liner geometry to be employed in these experiments are shown in Fig. 19. The start of the FRC formation and injection into the liners is held off until the liner has moved in a little over half way at 40 \( \mu\text{sec} \) (see Fig. 18). It requires only a few microseconds to form and insert the FRC. For that short duration, the liners only move inward \( \sim 4 \text{ mm} \) so that the stationary liner assumed in the 2D MHD calculation is a good approximation. A plot of the ion and electron temperature for the deuterium plasma from the calculation is found in Fig. 20. The peak plasma density under the liners at 44 \( \mu\text{sec} \) is \( 5x10^{21} \text{ m}^{-3} \). The axial magnetic field inside the liners before and after FRC insertion is 0.2 T and 1.2 T respectively reflecting the flux compression due to the presence of the high \( \beta \) FRC.

The primary diagnostic of plasma compression and heating will be the neutron count from the D-D fusion reaction. The yield is a sensitive measure of ion temperature. The signal will be analyzed using MCNP codes used in previous FRC experiments.\(^{20}\) A 16 channel time resolved Doppler spectrometer will be employed to confirm the plasma ion temperature as long as there is a gap between the liners. It is hoped to leave a small gap through the peak implosion to provide more data as to the final FRC plasma state. Through this same gap the plasma density will be obtained from a cross-chamber HeNe laser-based interferometer. With the liner compression of the axial magnetic field and FRC to 200 T, the final ion and electron temperature (the high plasma density will assure that \( T_e = T_i \) at that time) is given by the adiabatic scaling law (see Fig. 5) i.e., \( T_i + T_e \) (final) = \( T_i + T_e \) (initial)\( \times (B_f/B_i)^{85} = (500 \text{ eV})\times(60) \), or \( T_i = 15 \text{ keV} \) which would be well inside the parameter space needed for high fusion gain in a D-T plasma (5 - 20 keV). Such a result would clearly validate this approach for obtaining an appropriate fusion plasma for fusion powered propulsion represented by the Fusion Driven Rocket.

![Figure 20. Time history of the average electron and ion temperatures in the FRC from the 2D MHD calculations during the formation and insertion of the FRCs into the converging liners.](image)

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